

Structure of the lecture

1. Dendritic physiology and integration

- 1.1 Dendritic morphologies
- 1.2 Voltage and current transmission
- 1.3 Biophysical computations in segregated dendrites
- 1.4 Dendritic spikes

2. Dendrites in computation

- 2.1 NMDA favors clustered vs sparse inputs
- 2.2 Minimal dendritic reductions
- 2.3 Memory consolidation in the dendrites
- 2.4 Dendritic information processing
- 2.5 ANN with dendrites

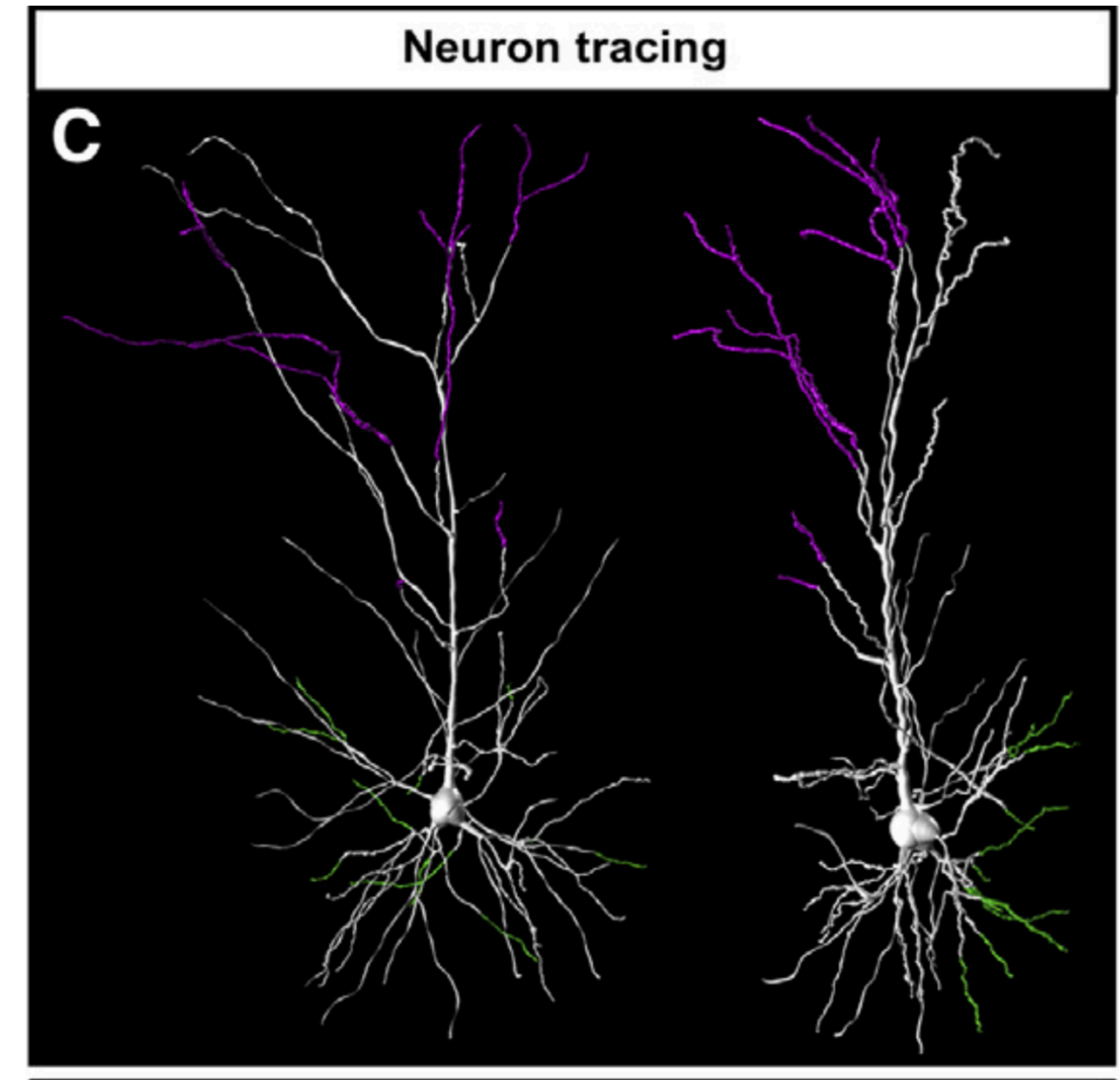


What are the dendrites?

Dendrites are the **branched extensions of neurons** that receive electrical signals from other neurons and convey this information toward the cell body.

Dendrites play a crucial role in neural communication by **increasing the surface area** available for synaptic connections.

The changes in dendritic membrane potential following a synaptic input, and the consequent flow of electrochemical currents from the dendrites to the cell's soma, are called **dendritic integration**.



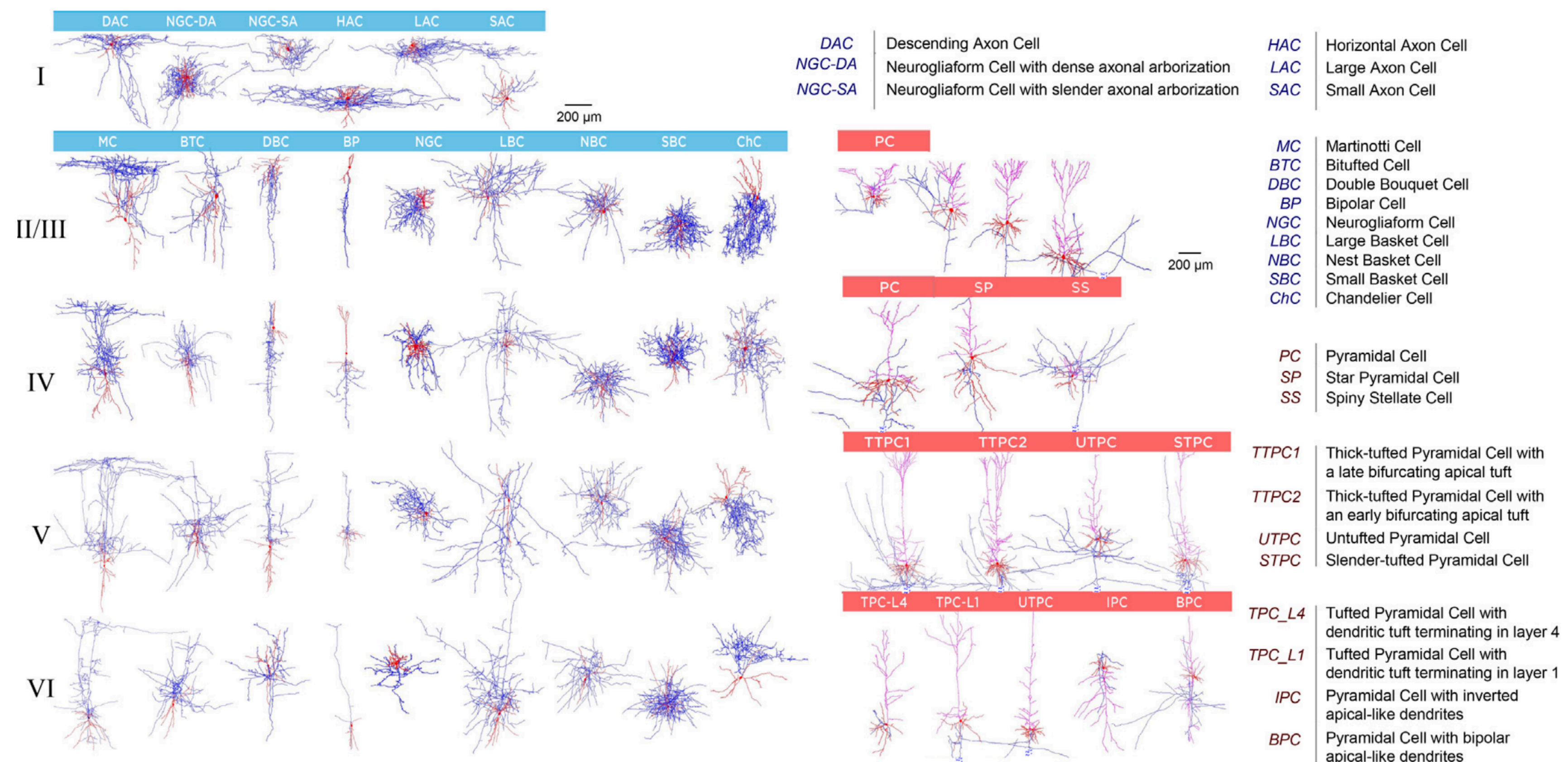
Dendritic morphologies

Dendritic structure changes with cell type

Cortical cells can be organized for their electrical, genetic, and morphological properties.

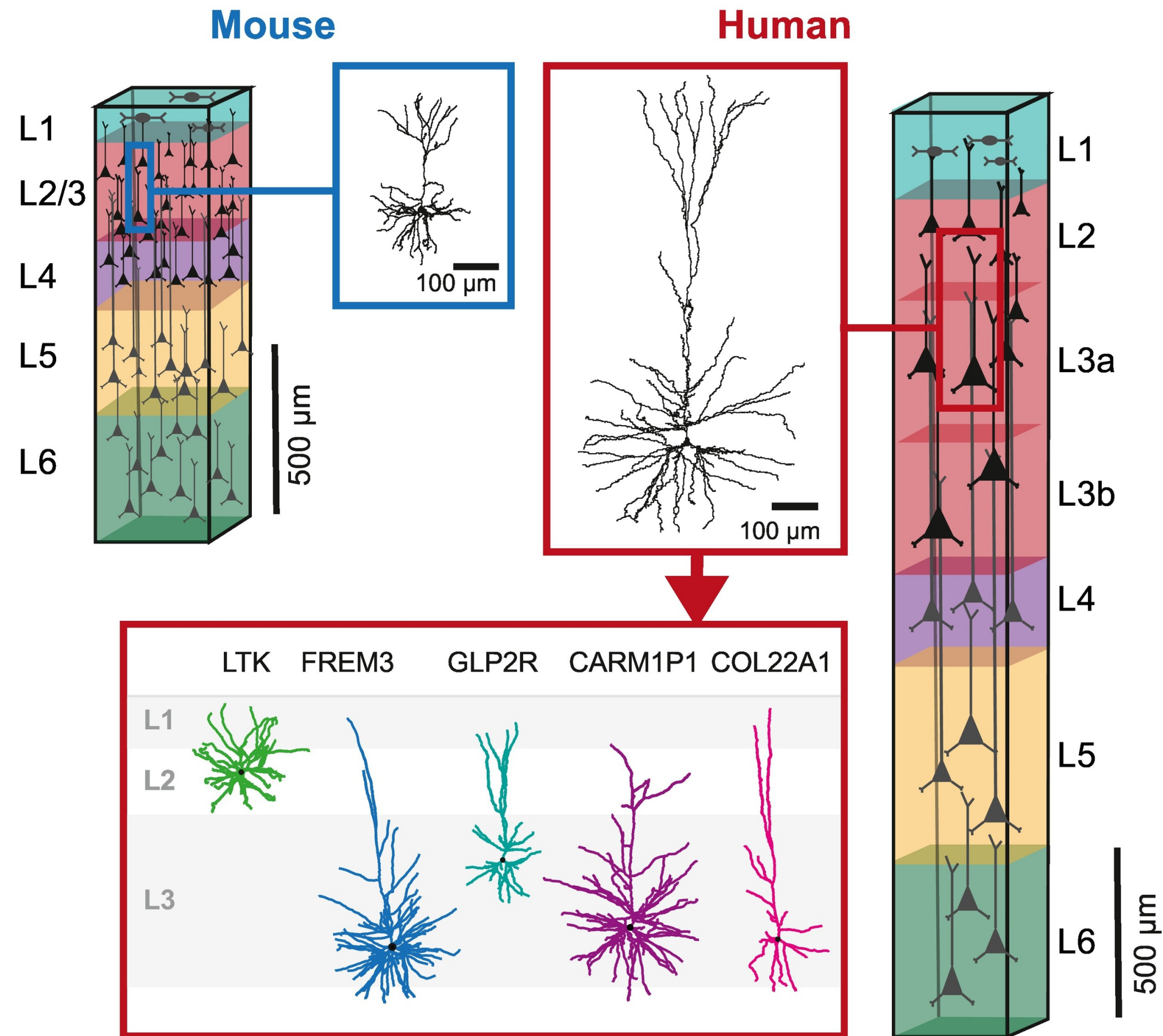
The morphology concerns the shape of the dendritic processes that extend from the cell body.

Does the dendritic structure impact how the cells integrate signals?



Dendritic morphologies

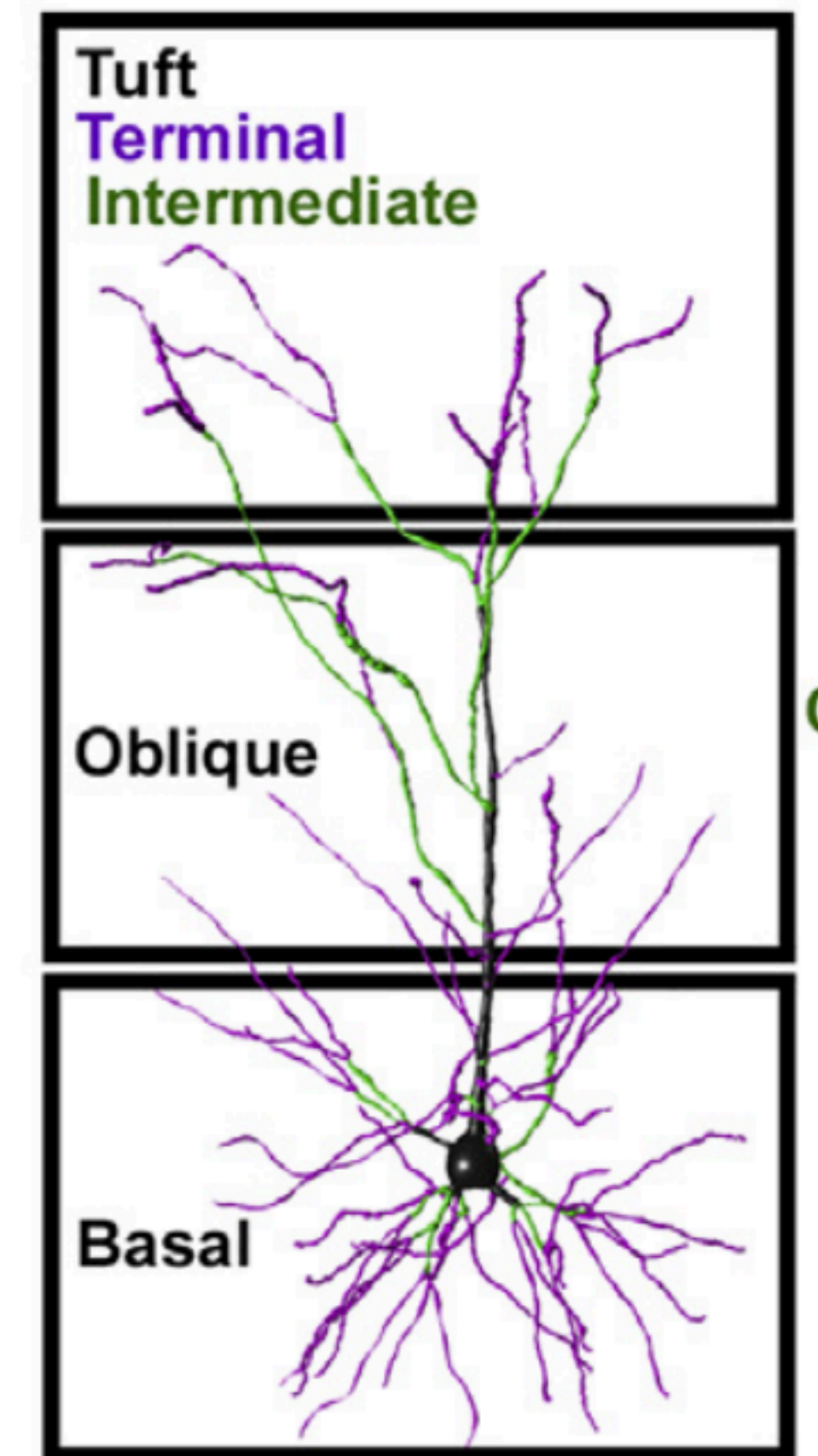
The backbone of cortical computation: the pyramidal cell



The pyramidal cells are the most abundant in the neocortex, about 70-80%.

Pyramidal cells' dendrites can be categorised according to their distance from the soma and their orientation in:

- Basal
- Oblique
- Apical tuft



Integration of electrical activity in the dendrites

Current flowing in one dimensional cable

The membrane potential in x at time t depends on:

$$V_i(x, t) - V_i(x + \Delta x, t) = R I_i(x, t)$$

$$\frac{\partial V_m}{\partial x}(x, t) = -r_a \cdot I_i(x, t) \quad r_a = R/\Delta x$$

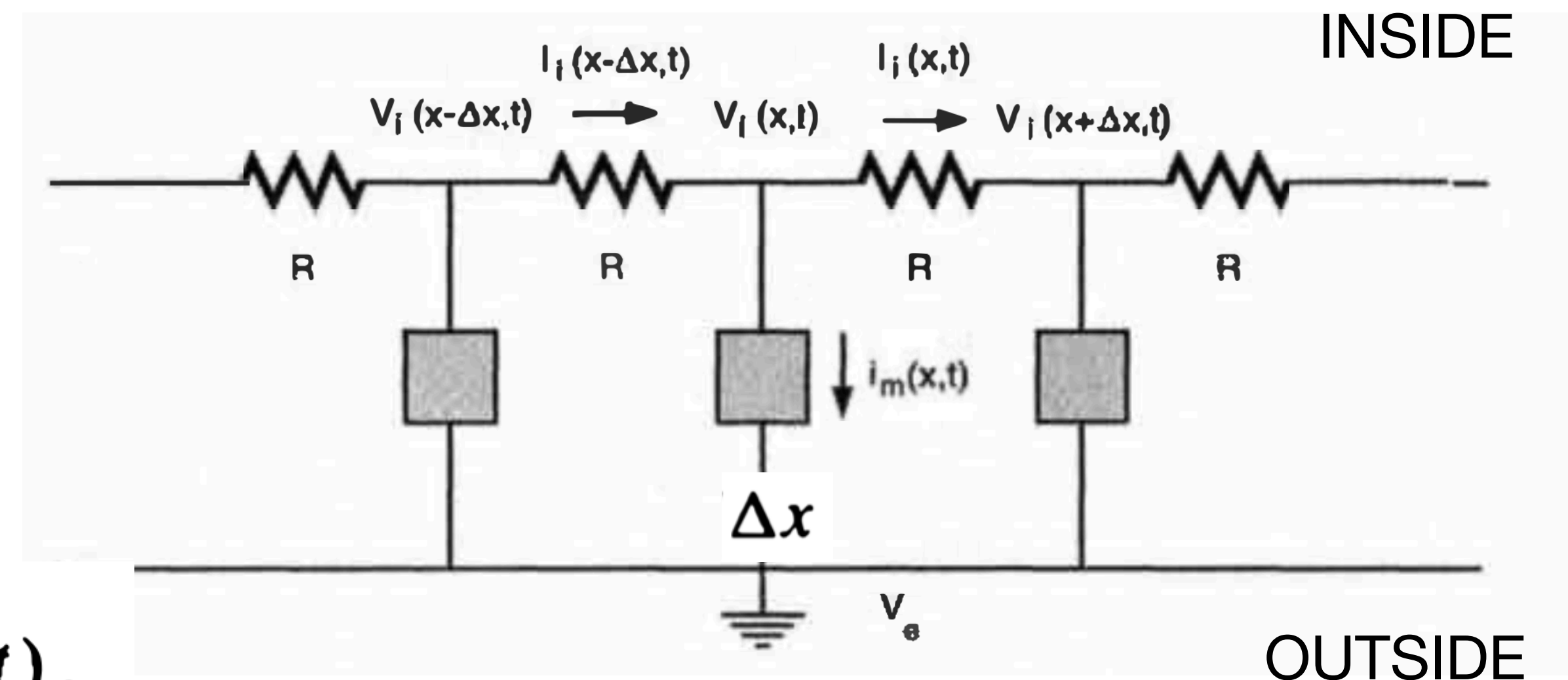
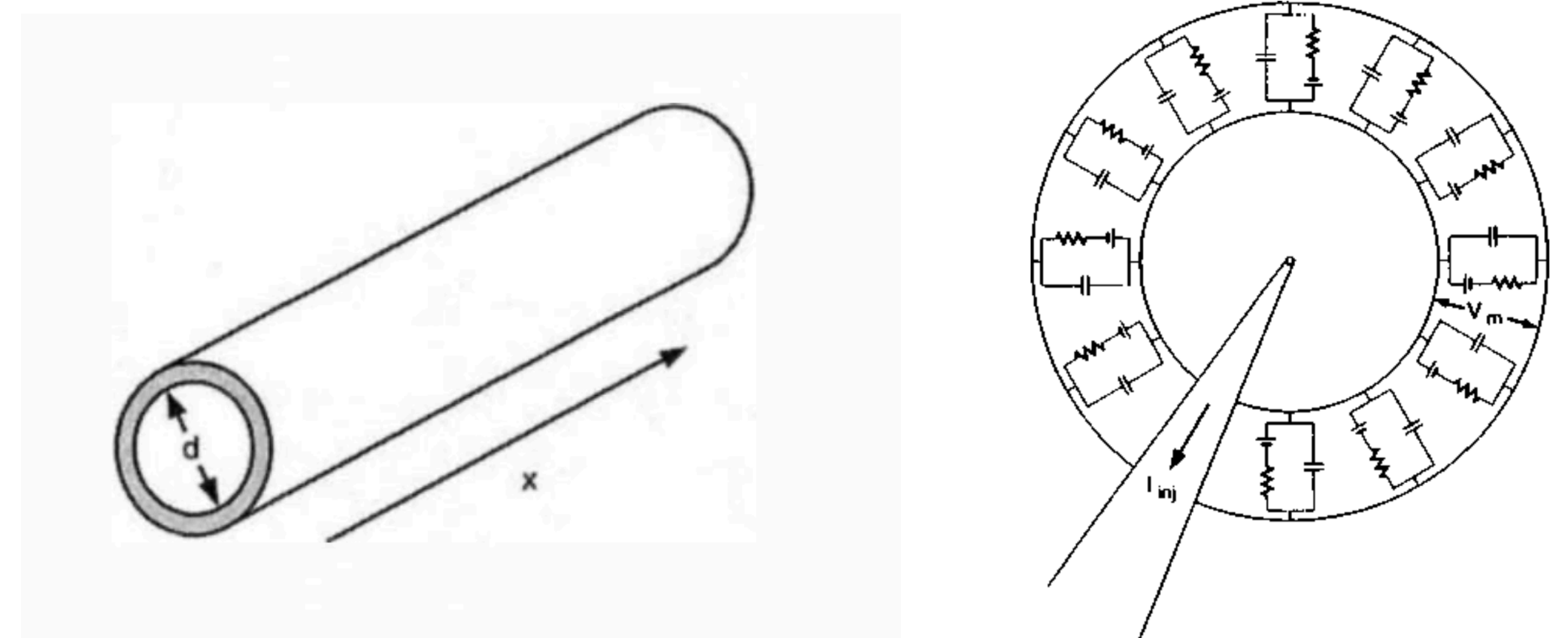
The density of current i_m is the current flowing *through* the membrane

$$i_m(x, t)\Delta x + I_i(x, t) - I_i(x - \Delta x, t) = 0$$

$$i_m(x, t) = -\frac{\partial I_i}{\partial x}(x, t).$$

Combining, we obtain

$$\frac{1}{r_a} \frac{\partial^2 V_m}{\partial x^2}(x, t) = i_m(x, t).$$



Integration of electrical activity in the dendrites

The infinitesimal membrane patch

Each segment is a membrane patch. The current flowing through is the HH membrane patch model.

$$i_m(x, t) = \frac{V_m(x, t) - V_{rest}}{r_m} + c_m \frac{\partial V_m(x, t)}{\partial t} - I_{inj}(x, t),$$

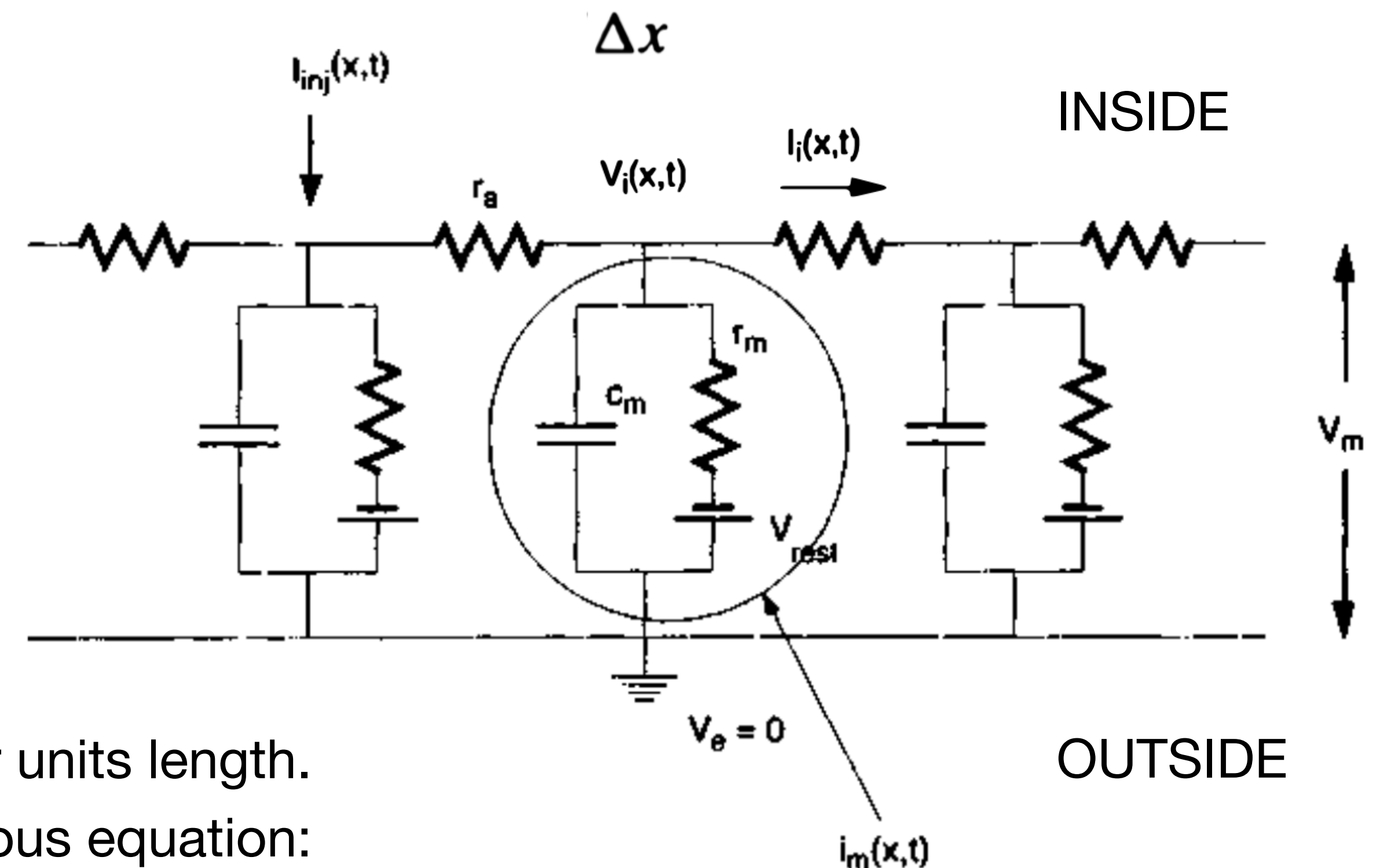
$$r_a = \frac{4R_i}{\pi d^2} \quad r_m = \frac{R_m}{\pi d} \quad c_m = C_m \cdot \pi d$$

The cable equation components are defined as quantity per units length.

The density of current i_m is the current substituted in previous equation:

$$\lambda^2 \frac{\partial^2 V_m(x, t)}{\partial x^2} = \tau_m \frac{\partial V_m(x, t)}{\partial t} + (V_m(x, t) - V_{rest}) - r_m I_{inj}(x, t),$$

$$\tau_m = r_m c_m \quad \lambda = (r_m / r_a)^{1/2}.$$



Integration of electrical activity in the dendrites

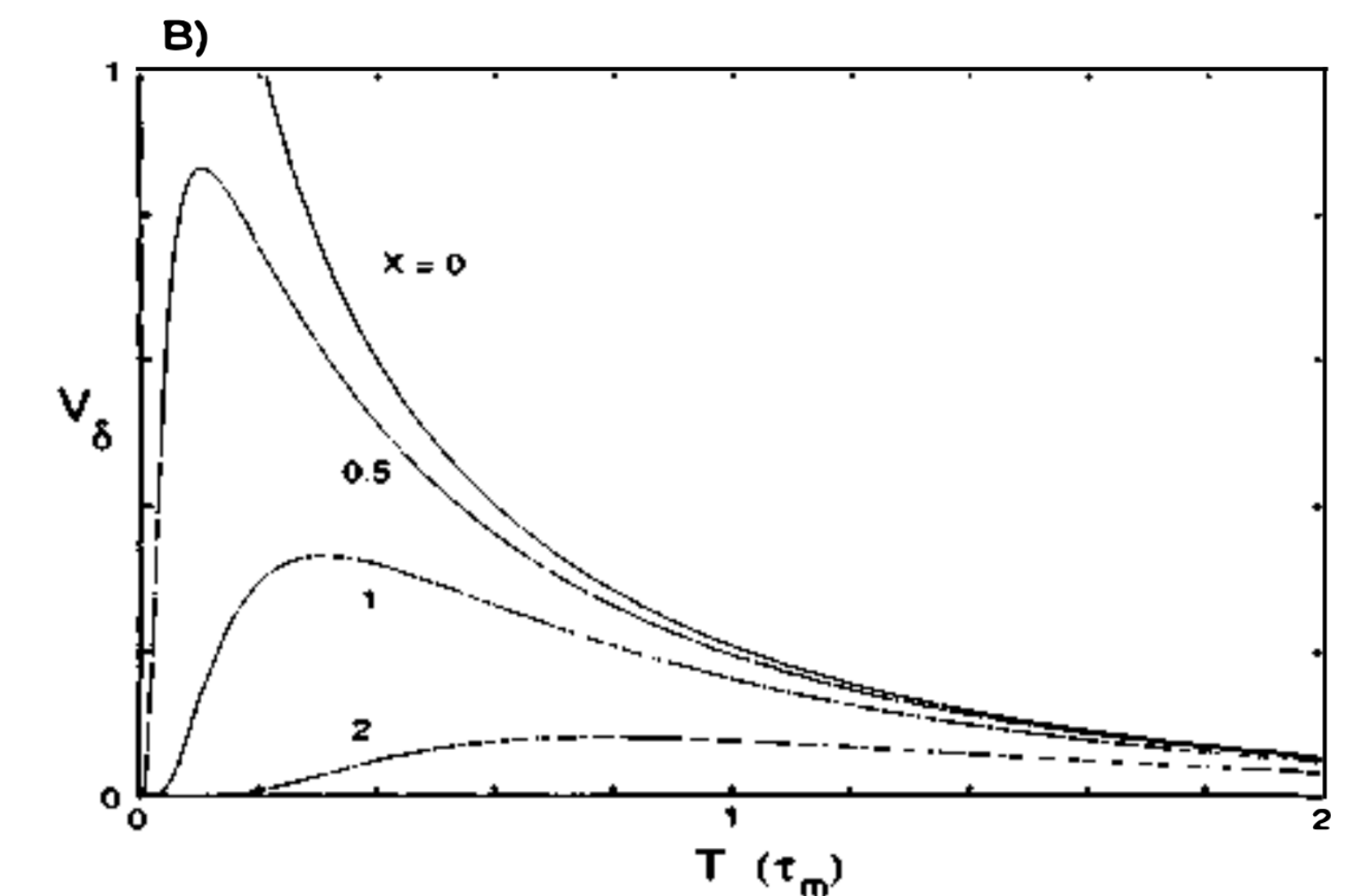
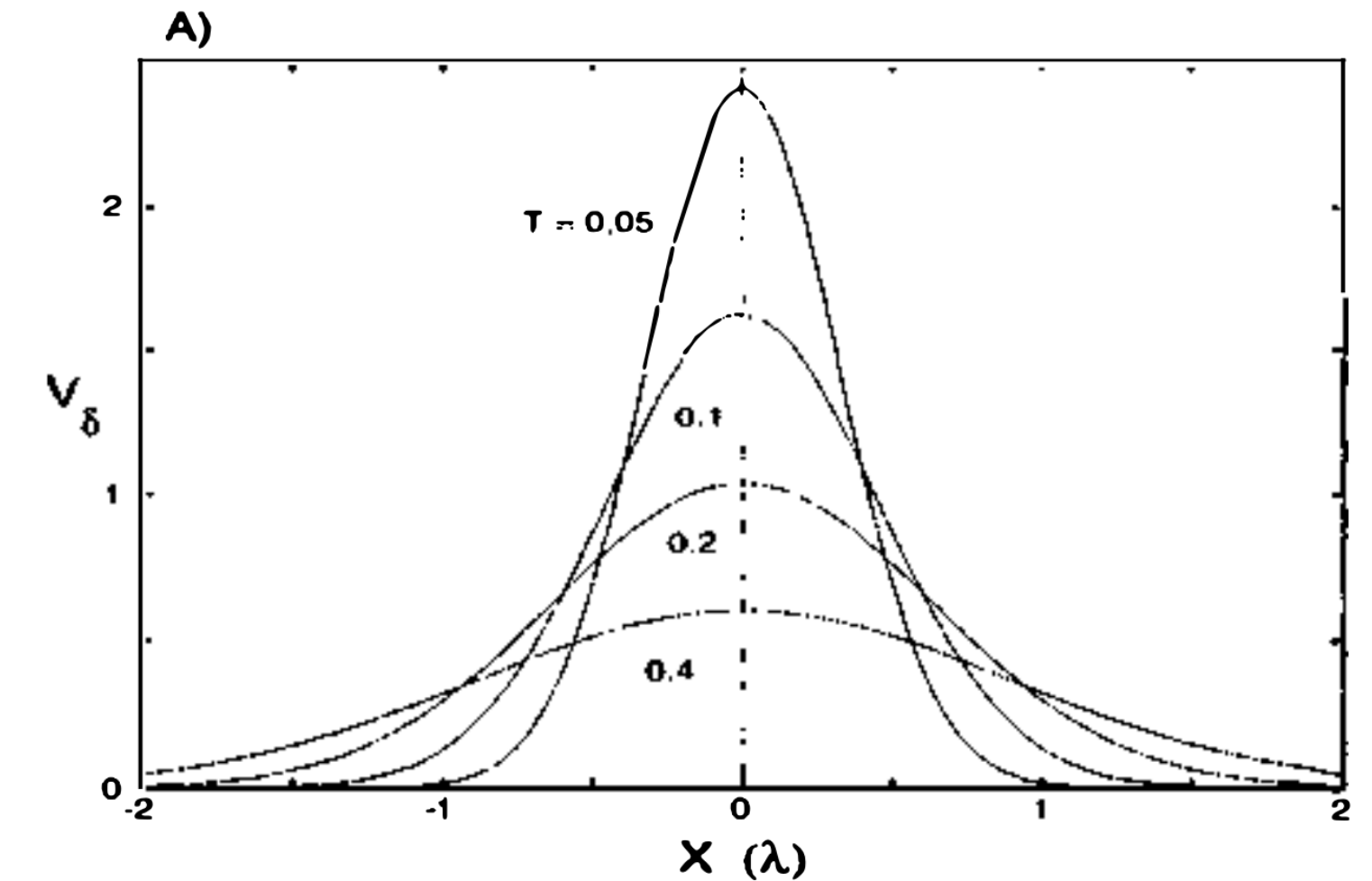
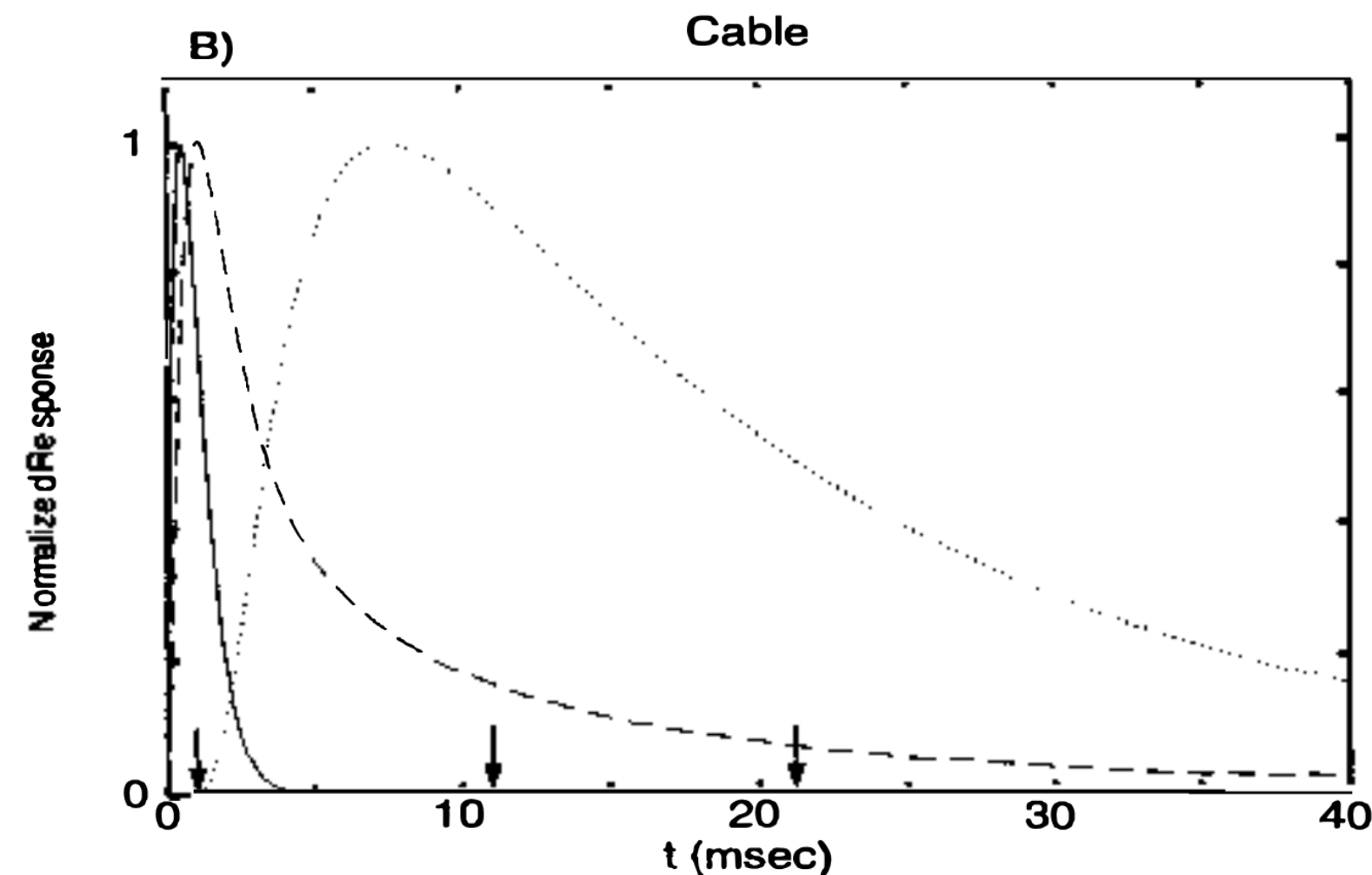
Segregated activity

$$\lambda^2 \frac{\partial^2 V_m(x, t)}{\partial x^2} = \tau_m \frac{\partial V_m(x, t)}{\partial t} + (V_m(x, t) - V_{\text{rest}}) - r_m I_{\text{inj}}(x, t),$$

The direct consequences of the cable equation are:

1. the variation in membrane potential are transmitted with a delay.
To define the signal propagation speed we use measure the centroid of the time (see book, eqs. 2.43), and this result in a pseudovelocivity:

$$v = 2 \frac{\lambda}{\tau_m} = \left(\frac{d}{R_m R_i C_m^2} \right)^{1/2}.$$



Integration of electrical activity in the dendrites

Segregated activity

2. When a synaptic event leads to an inflow of current in the dendrites, the current is attenuated over time and space.

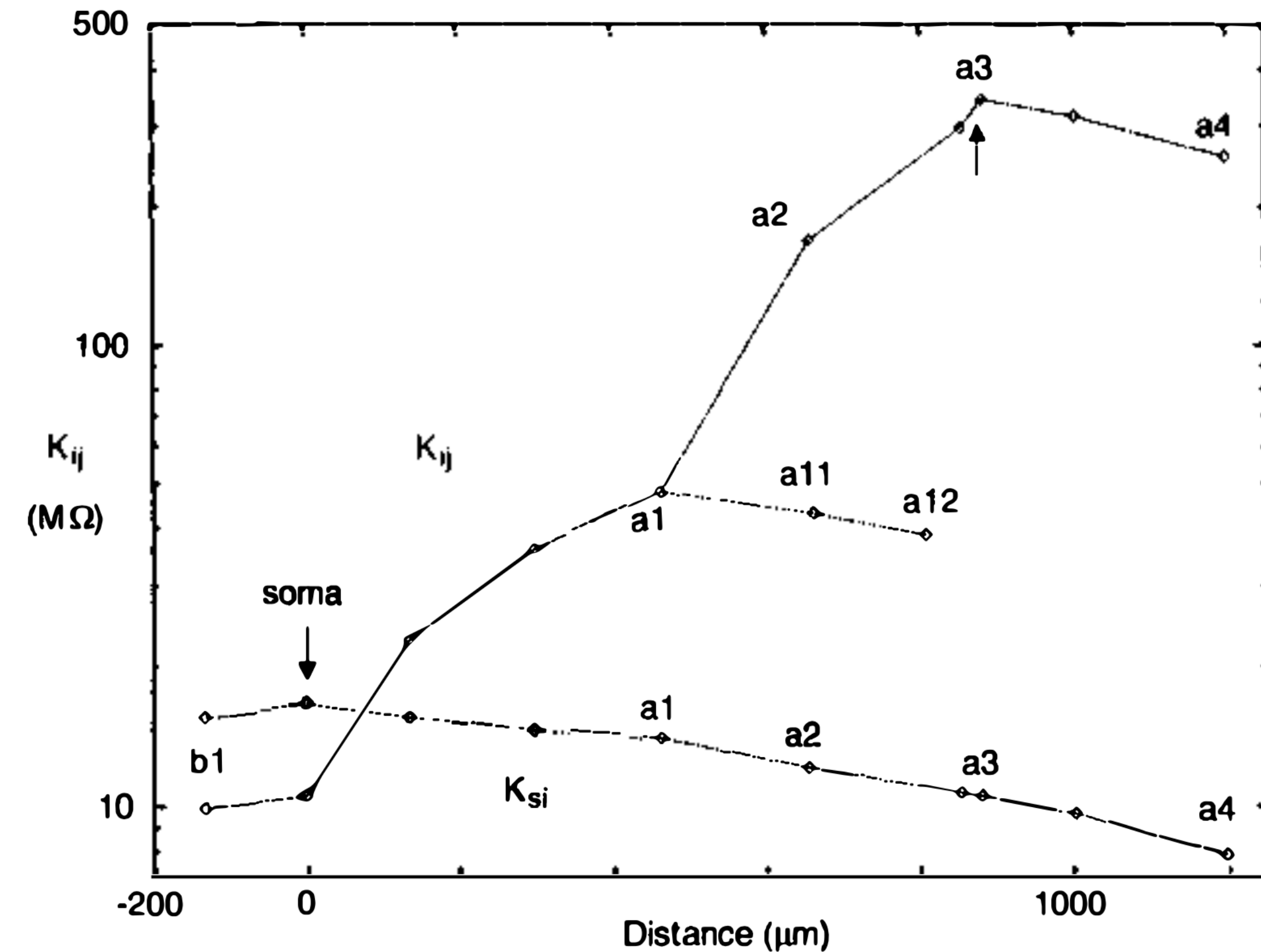
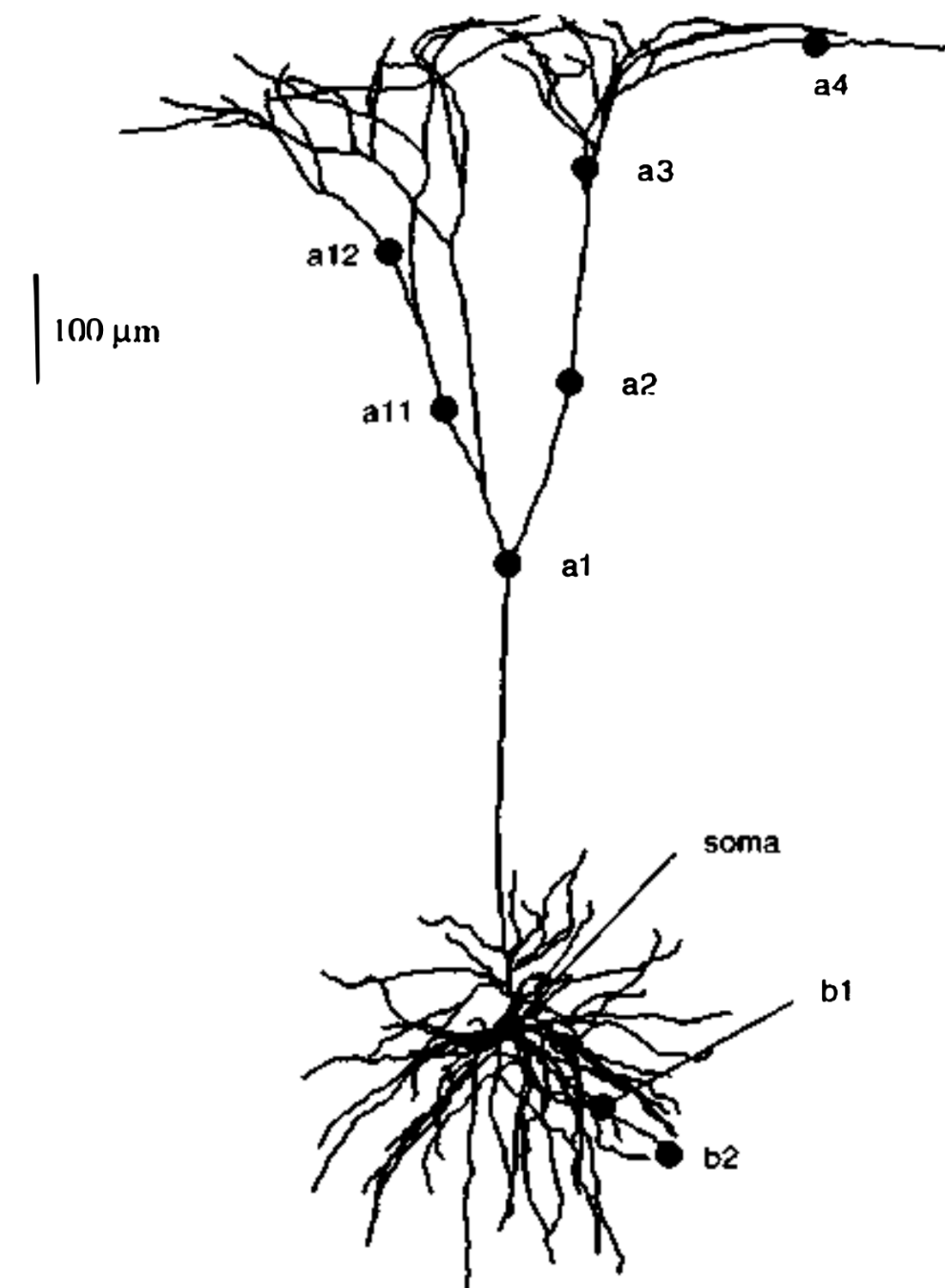
Same site - delayed

$$K_{ii}(T) = \frac{R_m}{2\pi d\lambda(\pi T)^{1/2}} e^{-T}$$

Different site - stationary input

$$\tilde{K}_{ij} = \frac{R_\infty}{2} e^{-|i-j|/\lambda}$$

$$R_{\infty,0} = \left(\frac{R_m \cdot R_i}{\pi^2} \right)^{1/2} \frac{2}{d_0^{3/2}}$$



Biophysical computations in segregated dendrites

Passive dendrites

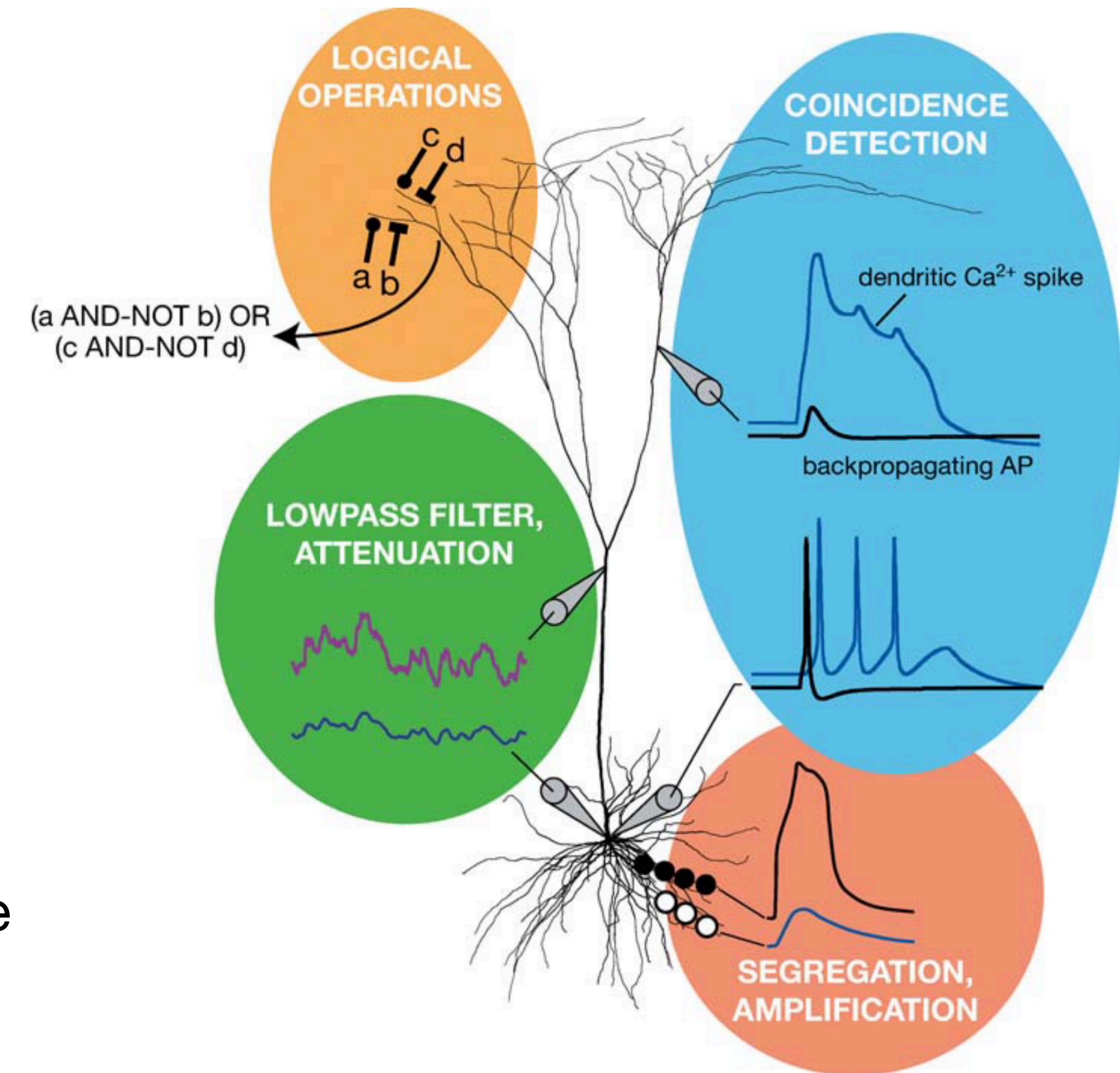
The passive properties of the dendritic tree are the backbone of dendritic computation.

- **Delay lines via dendritic filtering**

This filtering tends to attenuate the dendritic signal as a function of the distance it travels and the frequency of the original signal.

- **Parallel processing and local computations**

Spatial proximity leads to a nonlinear interaction between multiple synaptic inputs if they colocalize in time and space. Dendrites enable the spatial separation of inputs to minimize their interaction.



Synaptic interaction in a passive tree

Shunting inhibition - recall from previous class

Synaptic input acts to change the membrane conductance.

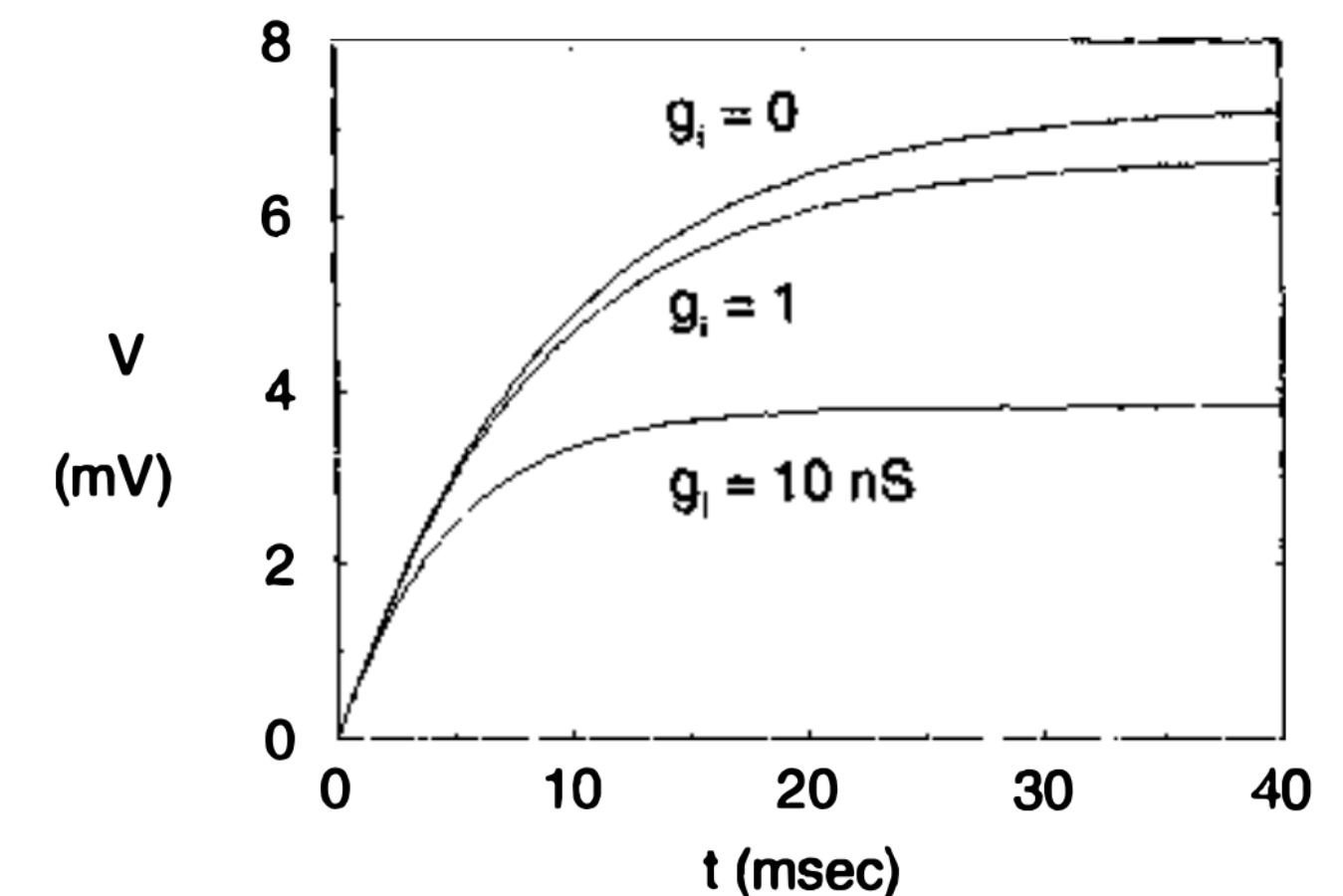
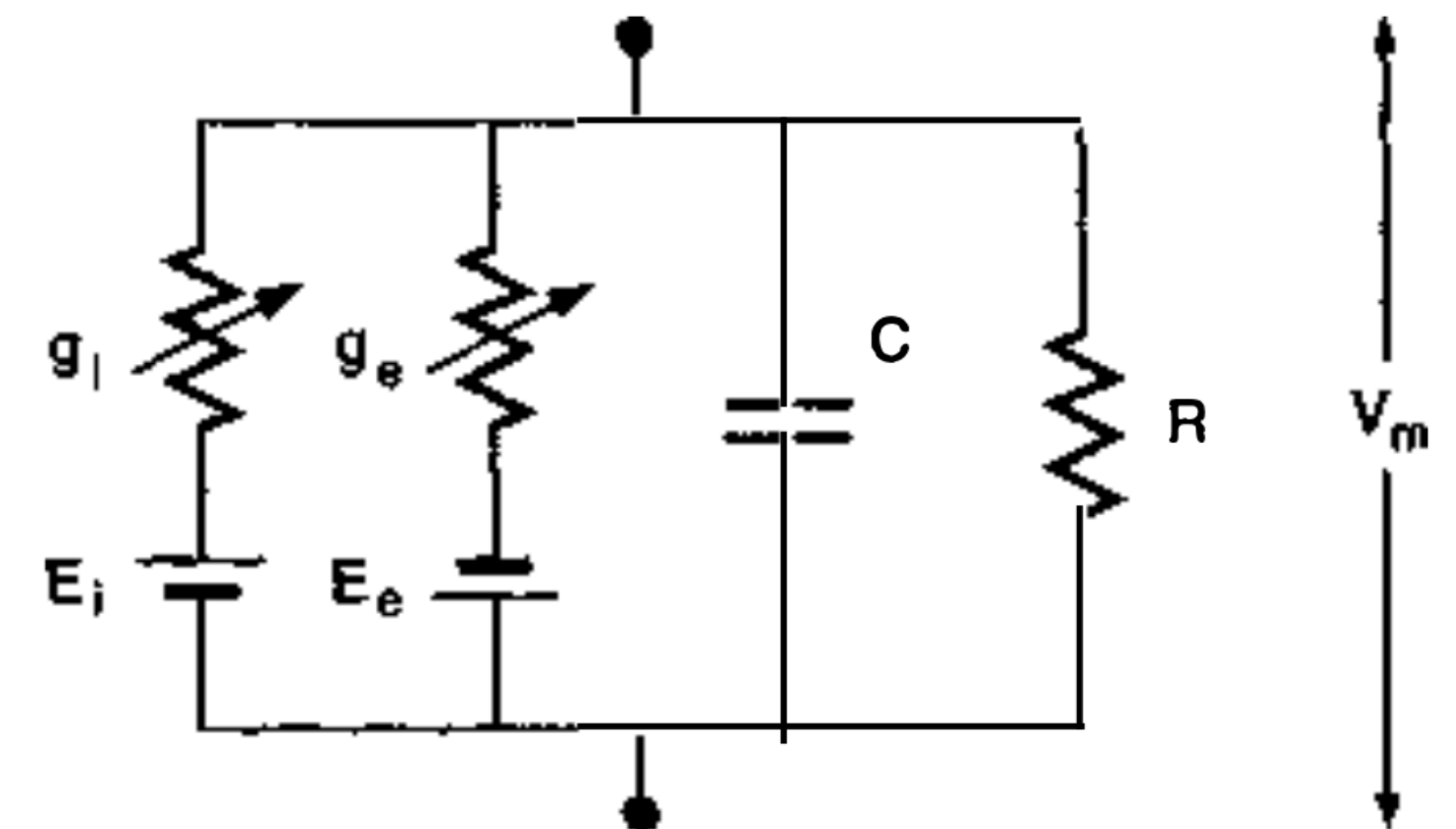
$$I_{\text{syn}}(t) = G_{\text{syn}}(t)[V_m - E_{\text{syn}}]$$

The change in membrane voltage caused by two or more synaptic inputs is not the sum of the voltages induced by the individual synaptic inputs.

A classical effect of this interaction is **shunting inhibition**, where inhibition has a divisive effect on the total input current

$$V_{\infty} = \frac{g_e R E_e}{1 + g_e R + g_i R} \approx \frac{g_e E_e}{g_i}$$

$$C \frac{dV}{dt} = g_e(E_e - V) - g_i V - \frac{V}{R}$$



Synaptic interaction in a passive tree

Shunting inhibition in the dendritic tree

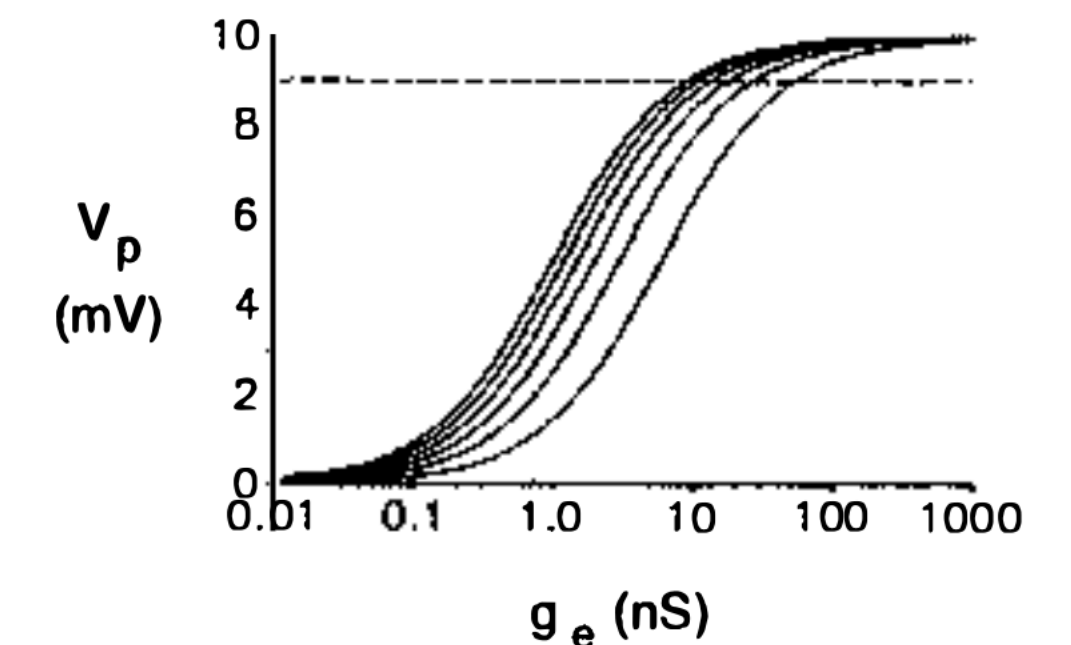
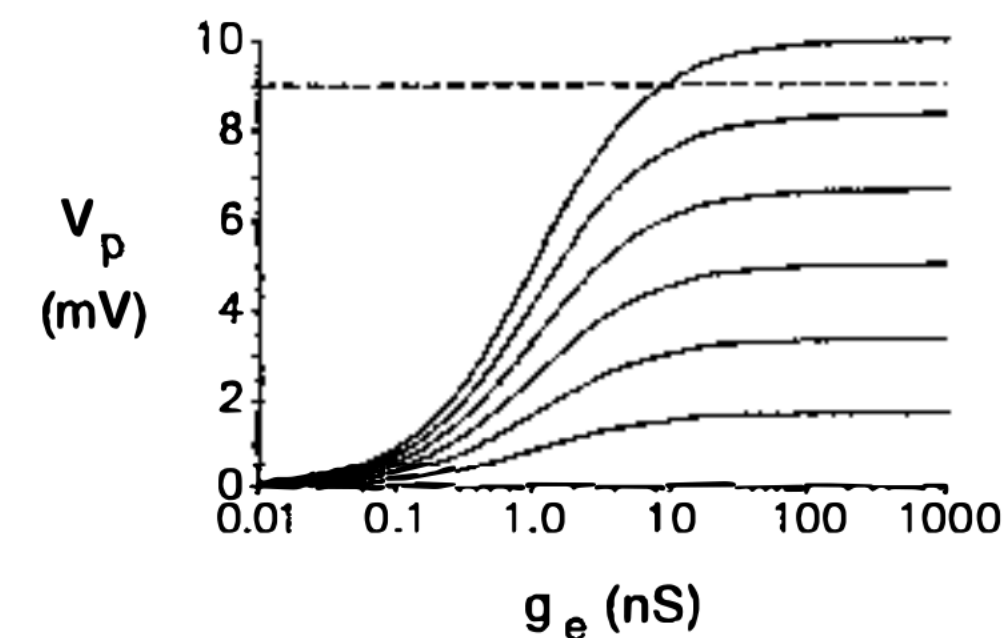
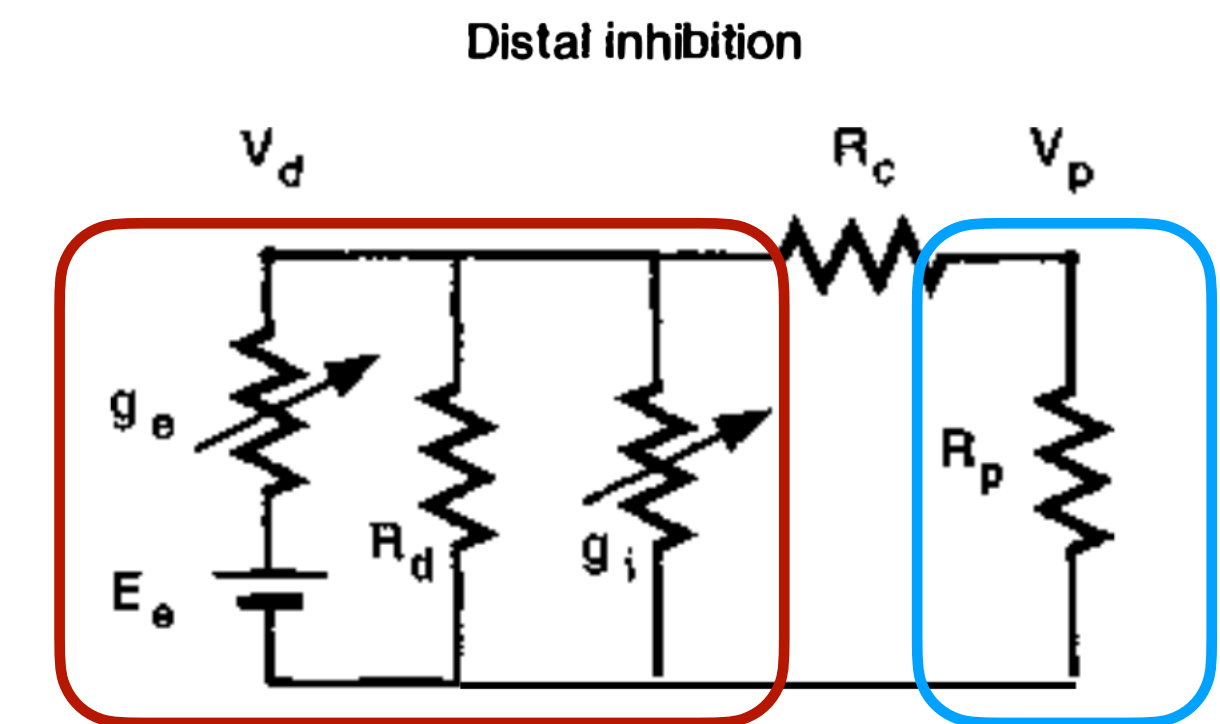
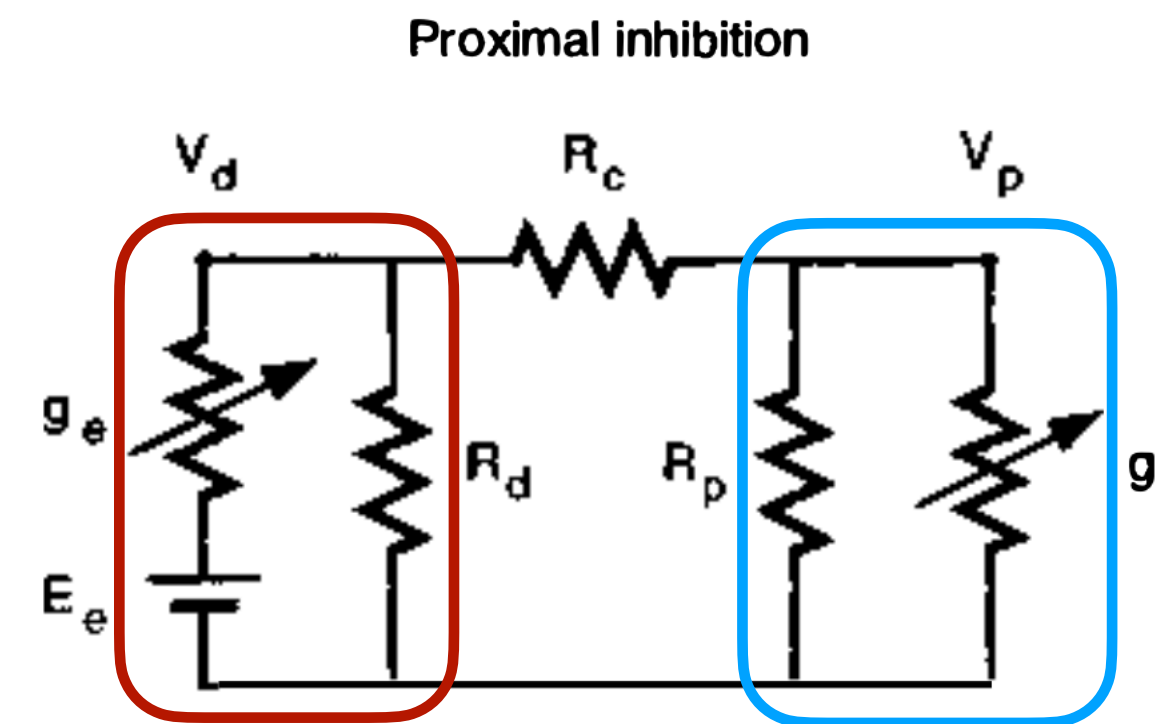
Let's now consider the case in which the **dendrite** is a single compartment, attached to the **soma**.

If excitation is distal and inhibition is proximal, inhibition acts as **absolute suppression**.
Independent of the strength of the input:

$$\lim_{g_e \rightarrow \infty} V_p = \frac{E_e R_p}{R_p + R_c + g_i R_c R_p}$$

If excitation and inhibition are both distal, excitation can overcome inhibition, that acts as **relative suppression**

$$\lim_{g_e \rightarrow \infty} V_p = \frac{E_e R_p}{R_p + R_c}$$



Synaptic interaction in a passive tree

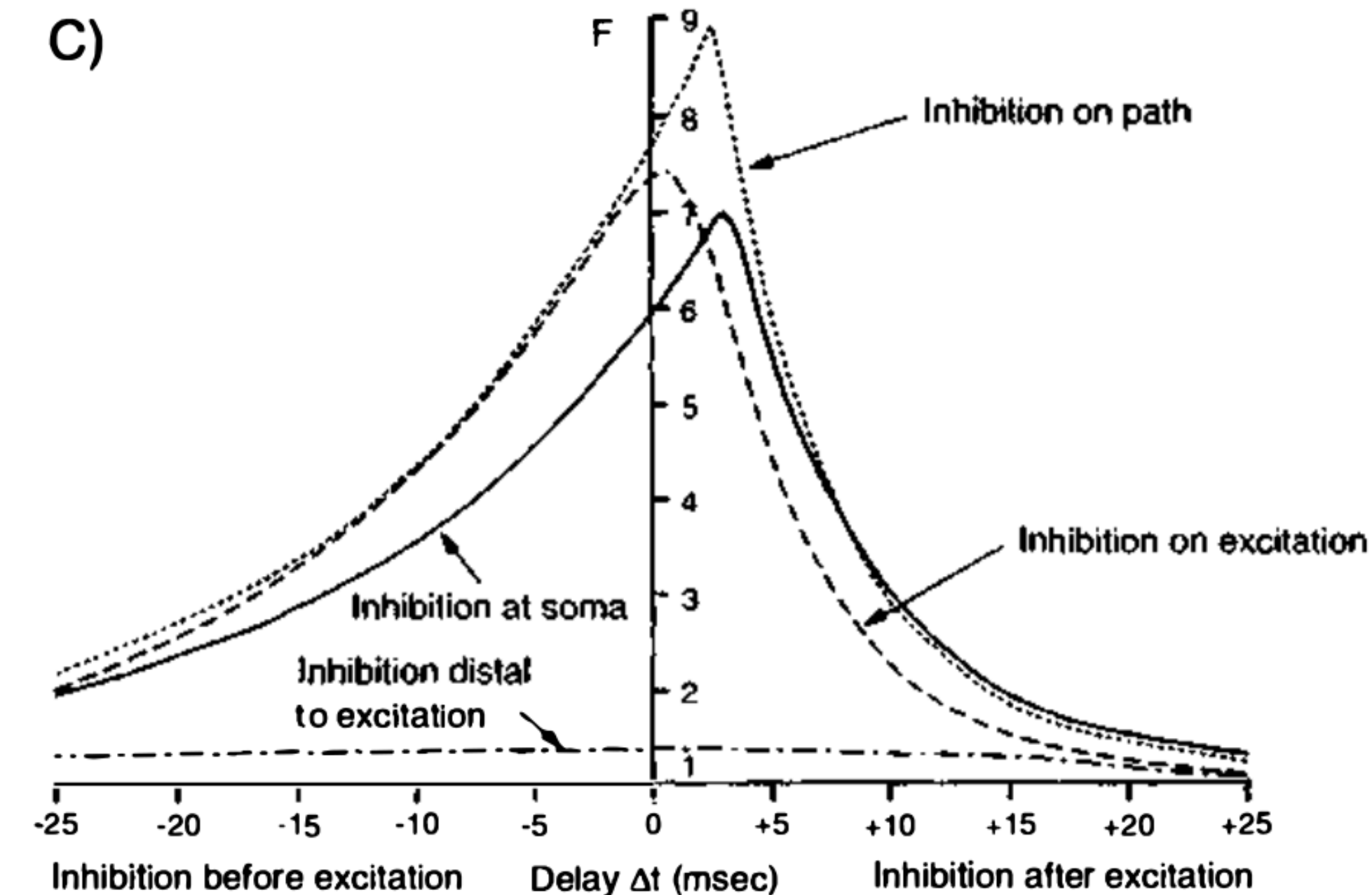
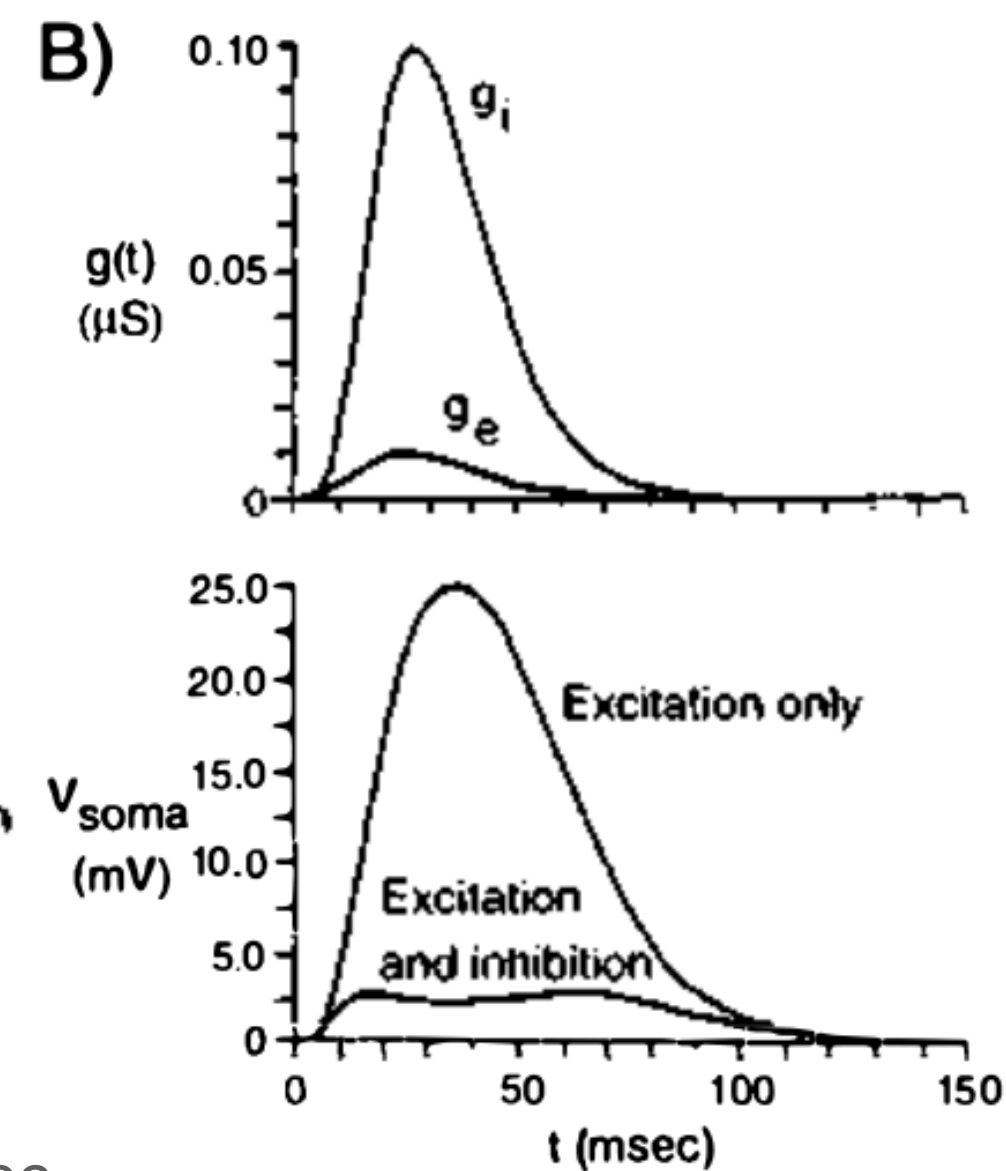
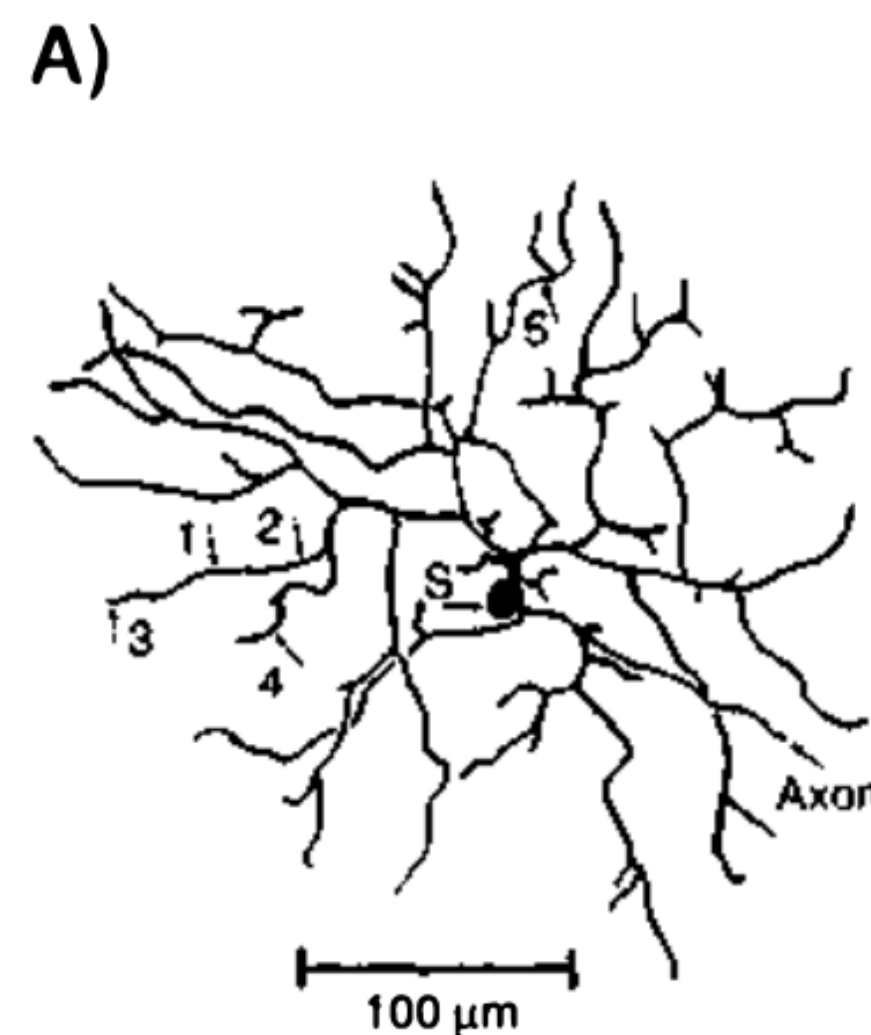
Shunting inhibition in the dendritic tree

This interaction can be generalized to any two points, introducing the F factor as the depolarization difference in presence of pure excitation or excitation and inhibition

$$F = \frac{g_e \tilde{K}_{es}}{1 + g_e \tilde{K}_{ee}} \cdot \frac{1 + g_e \tilde{K}_{ee} + g_i \tilde{K}_{ii} + g_e g_i \tilde{K}^*}{g_e \tilde{K}_{es} + g_e g_i \tilde{K}_e^+}$$

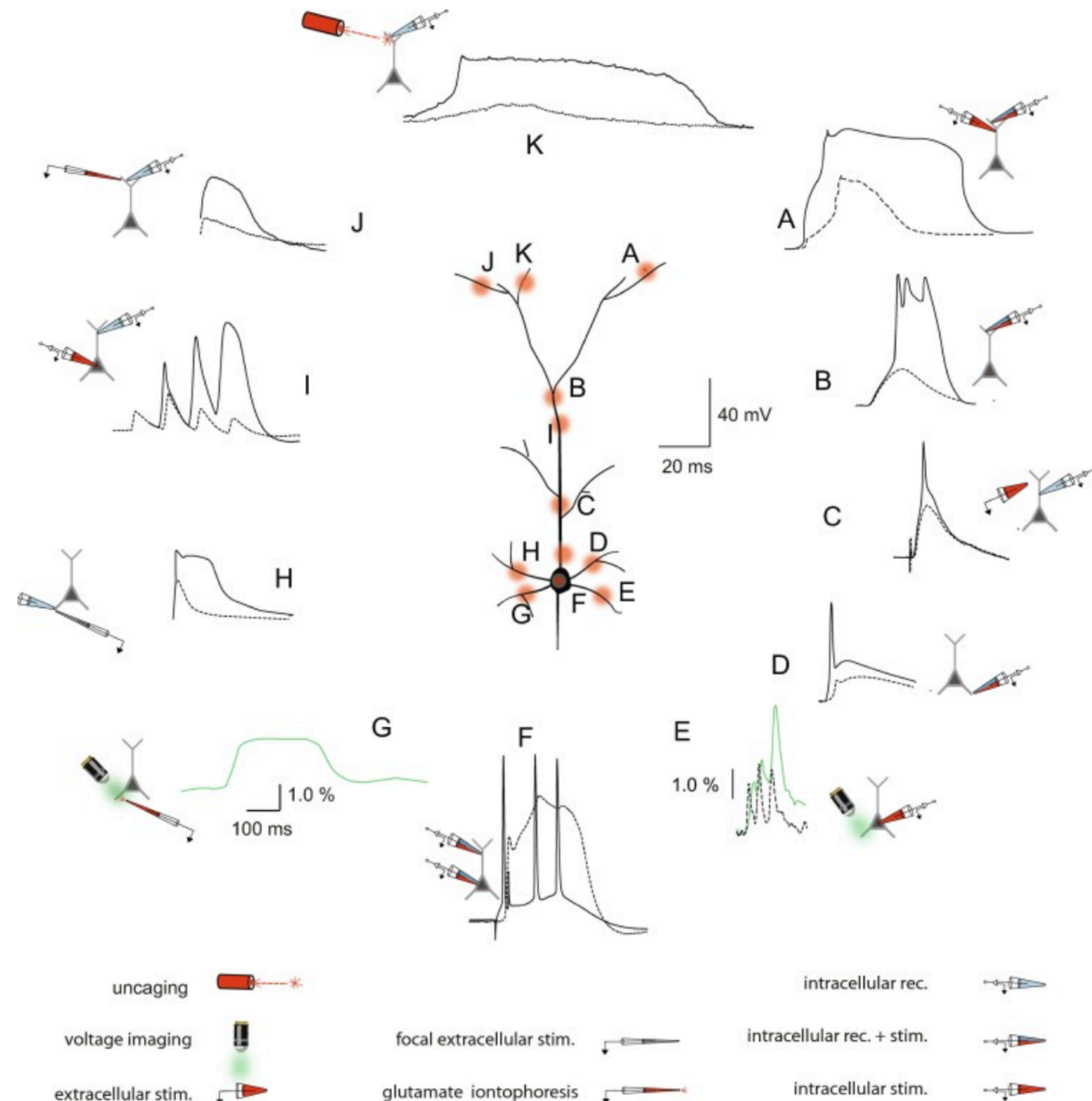
$$\tilde{K}_e^+ = \tilde{K}_{es} \tilde{K}_{ii} - \tilde{K}_{is} \tilde{K}_{ie}$$

$$\tilde{K}^* = \tilde{K}_{ee} \tilde{K}_{ii} - \tilde{K}_{ie}^2$$



Non linear integration and dendritic spikes

Dendritic spikes in pyramidal cells



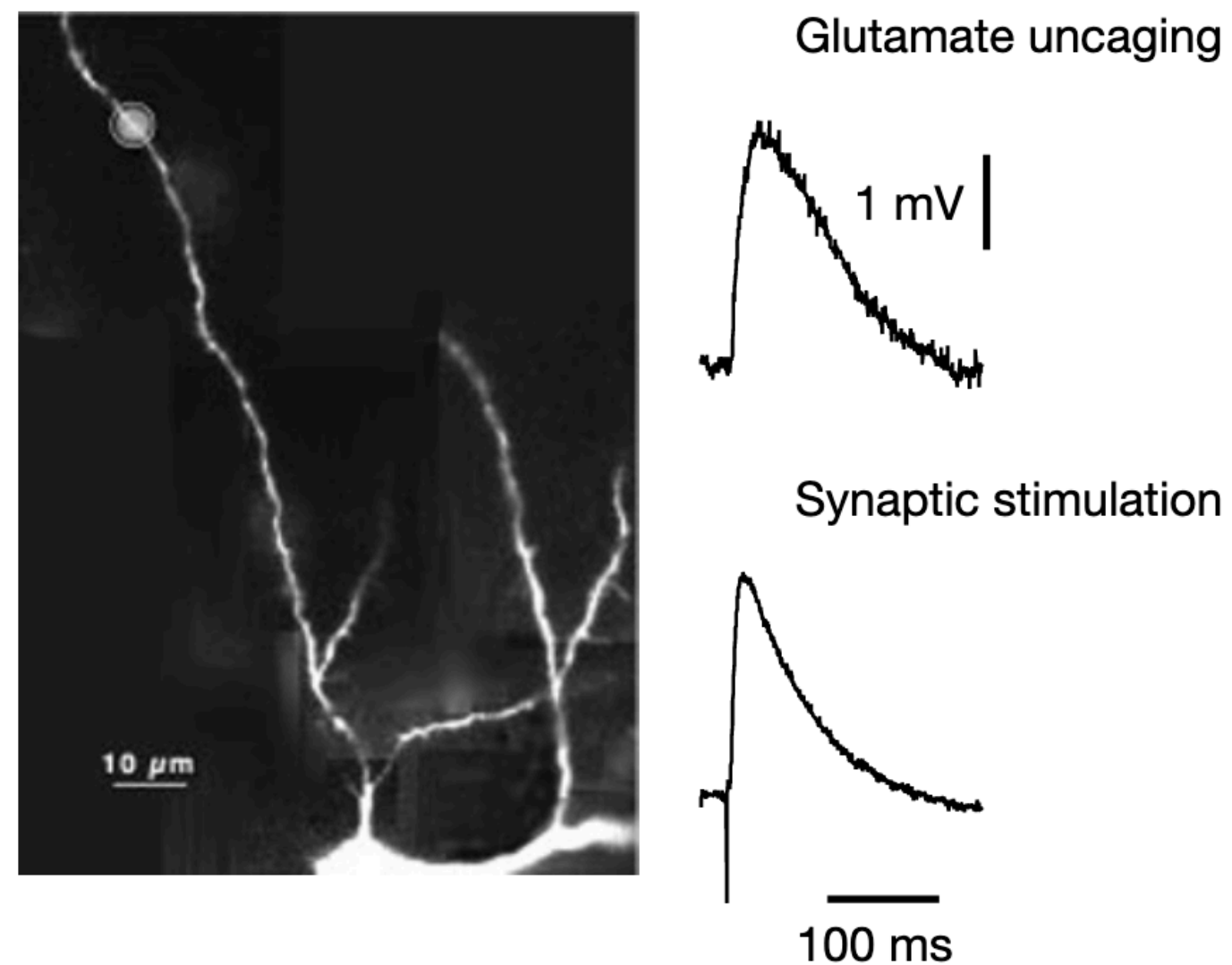
Dendrites exhibits voltage-dependent non-linear responses

The different classes of dendritic spikes vary significantly in duration, lasting between about a millisecond and hundreds of milliseconds:

- **Intrinsic spikes** are triggered when the dendritic membrane crosses a voltage threshold. These include: Na⁺ spikes/ spikelets, Ca²⁺ spikes, low-threshold spikes (LTS), and Ca²⁺ plateau-potentials.
- **Synaptic spikes** consist of NMDA spikes and plateau potentials, and NMDAR-dependent Ca²⁺ spikes.

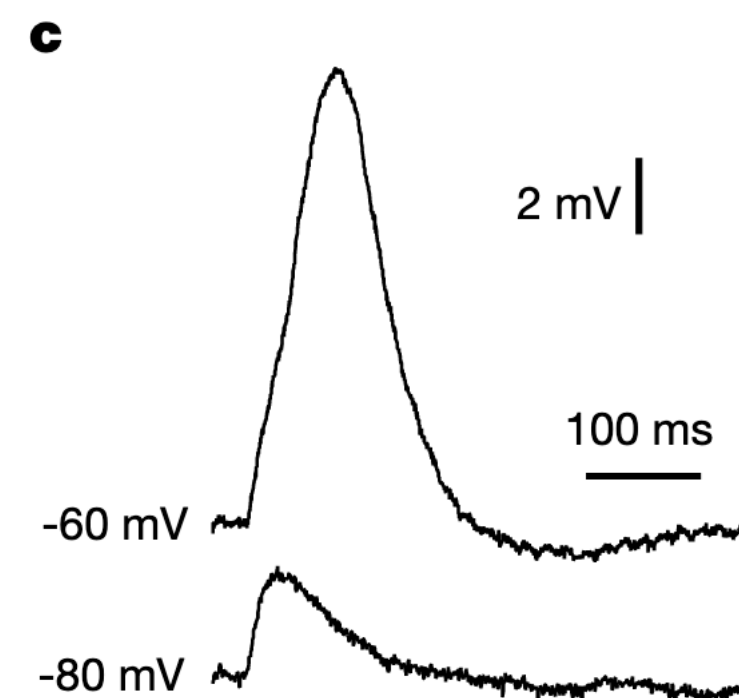
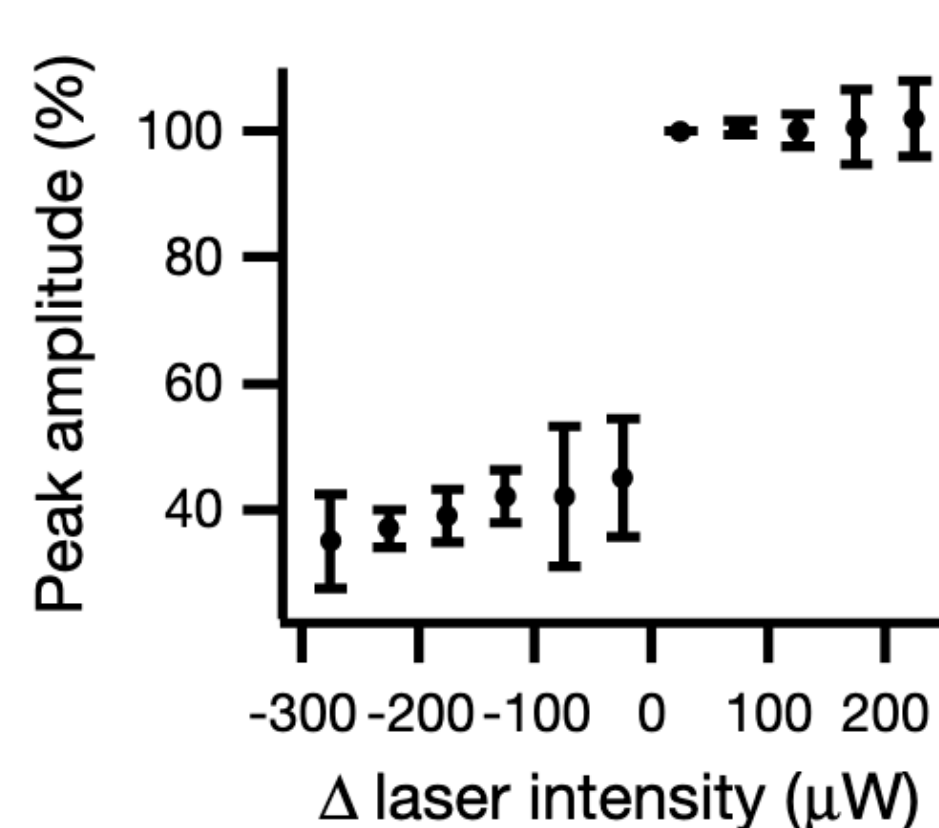
Non linear integration and dendritic spikes

Voltage-dependent NMDA receptors lead to dendritic Calcium spikes



Experiment with glutamate uncaging and laser stimulation shows:

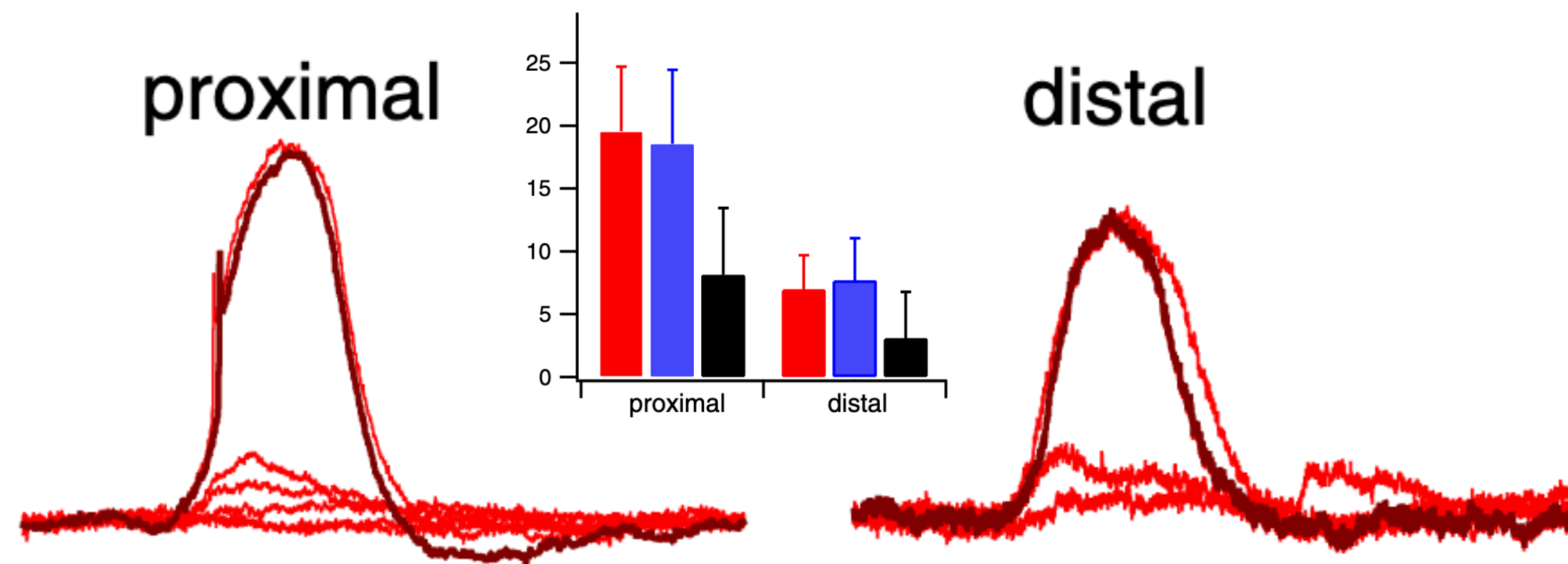
- Coactivation of clustered neighbouring basal inputs initiated local dendritic spikes;
- Results in ~ 6 mV (peak) and ~ 70 ms (half-width) voltage change at the soma, amplifying the somatic voltage response by 226%;
- The voltage threshold and all-or-none nature of the response indicated the initiation of local dendritic spikes;



These spikes were mediated mostly by **NMDA (N-methyl-D-aspartate)** receptor channels, which contributed at least 80% of the total charge.

Spatiotemporally Graded NMDA Spike/Plateau

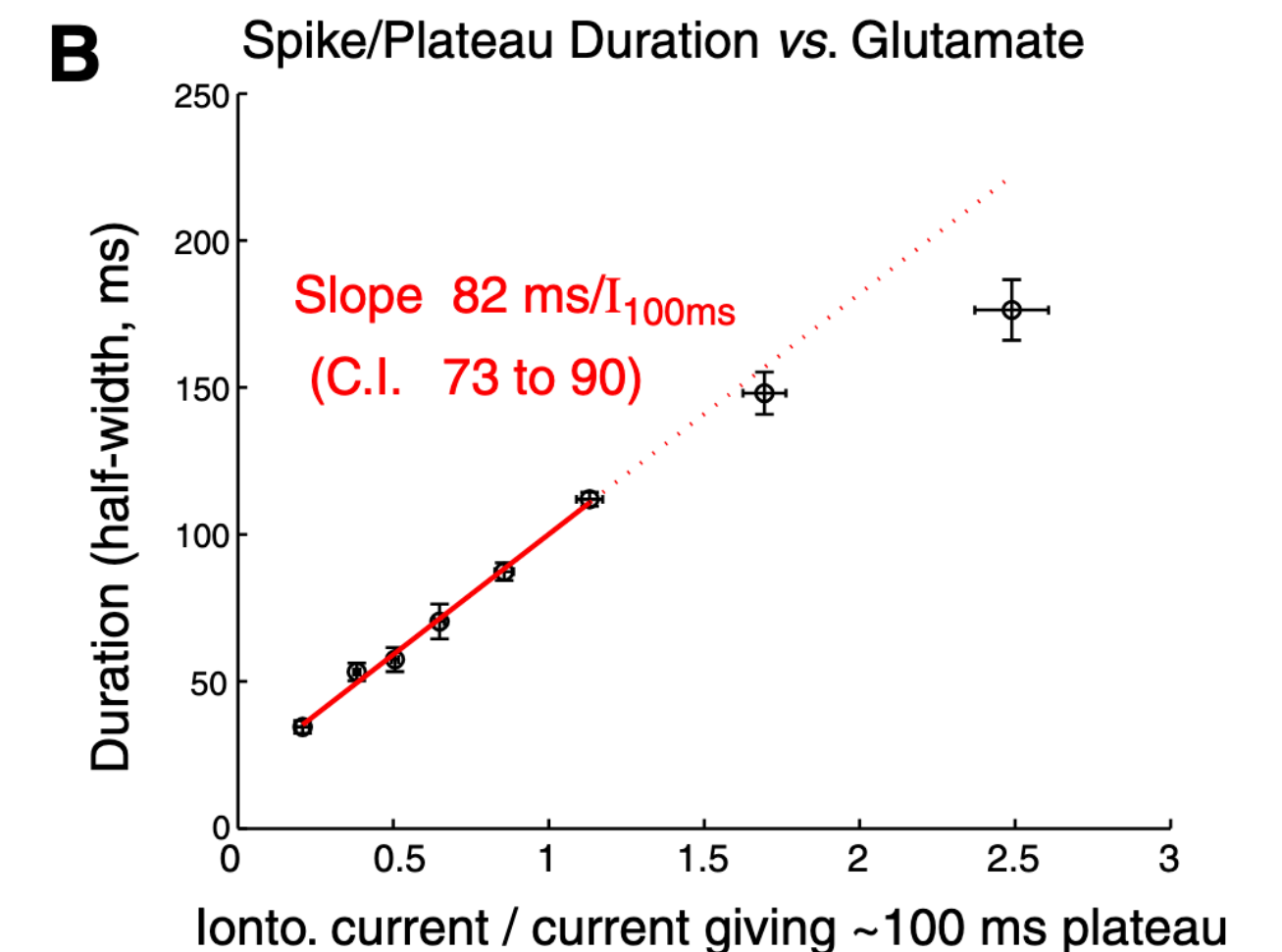
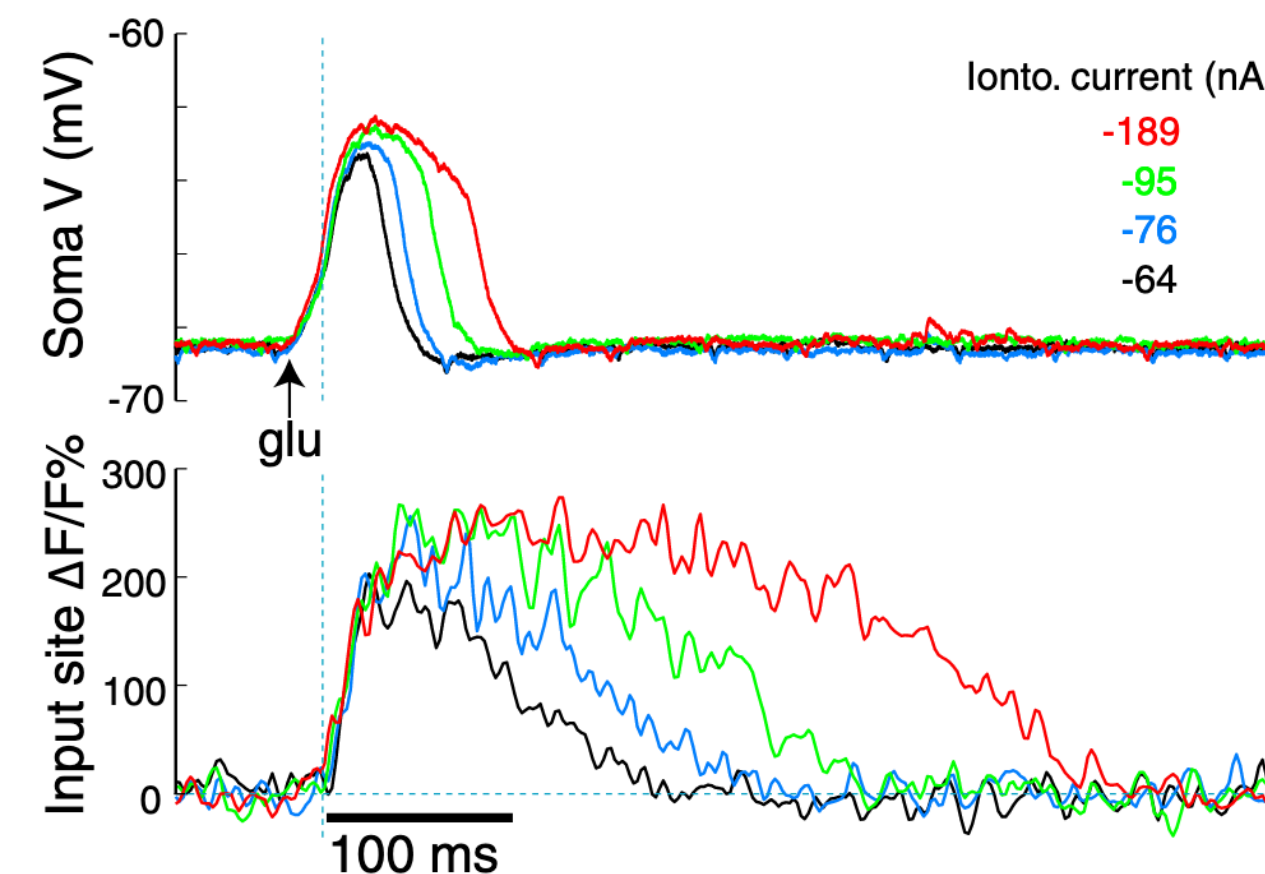
NMDA amplitude and duration depends on input location and strength



There is an 7x spatial gradient in average spike/plateau amplitude measured at the soma.

The threshold for NMDA spike grows from distal to proximal.

Spike/plateau duration grew with increasing glutamate and depolarization; high Ca²⁺ zone size grew with spike/plateau duration.

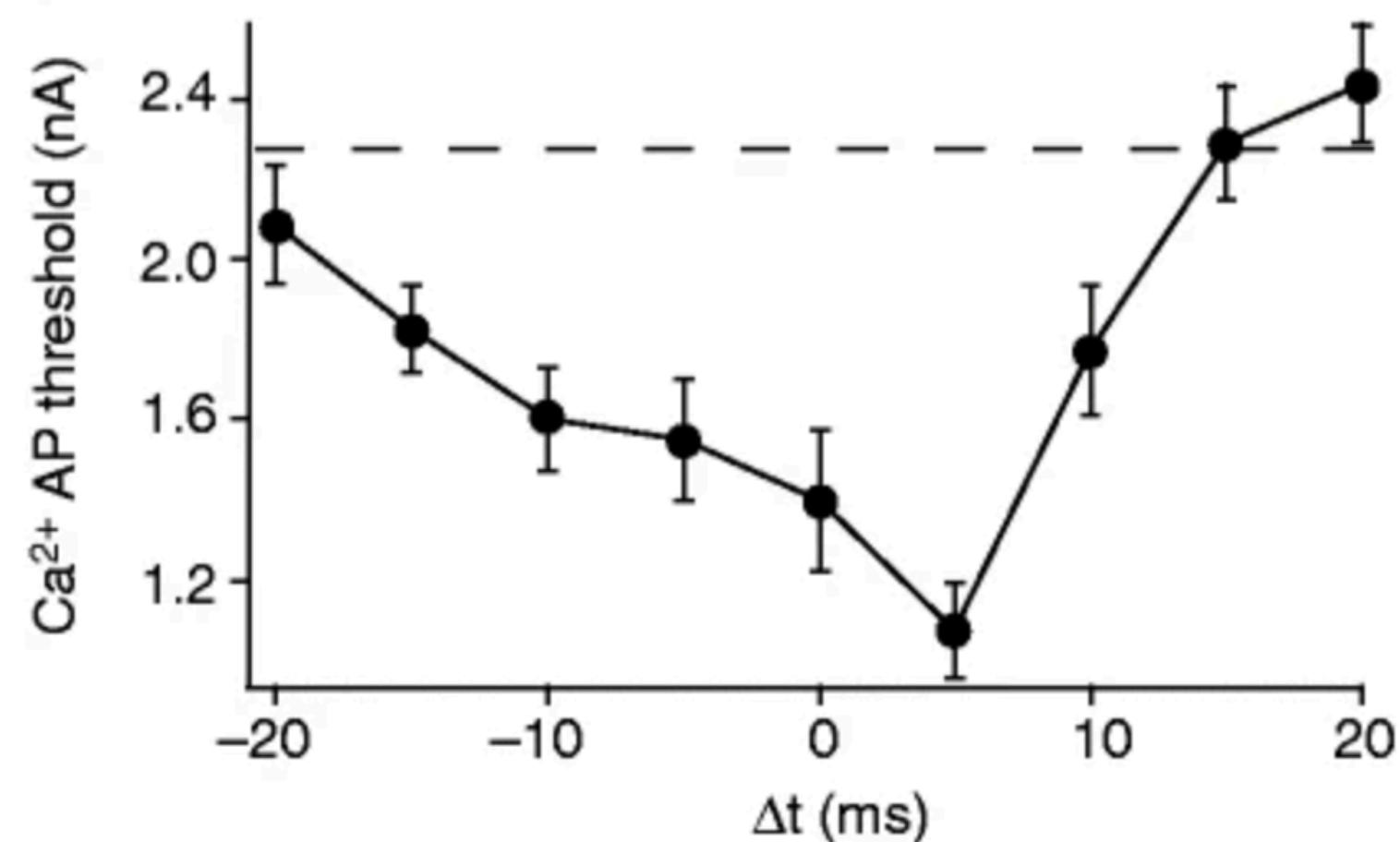


Back-propagating action potential

A cellular mechanism for coupling inputs arriving at different cortical layers

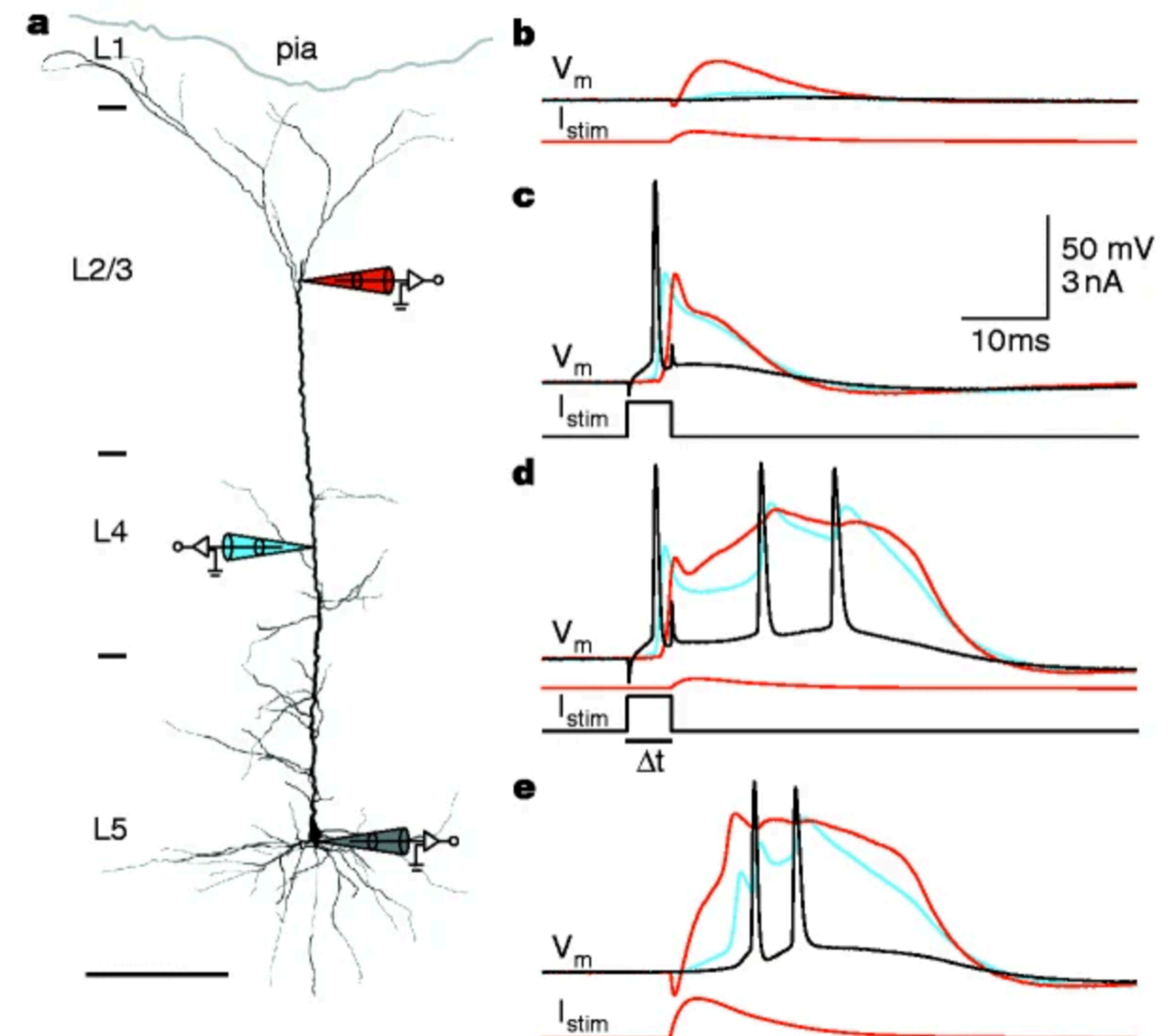
Distal dendritic inputs must cross a high threshold at the dendritic initiation zone to evoke calcium action potentials

They can then generate bursts of axonal action potential when they coincide with back-propagating sodium action potential generated in the axon.



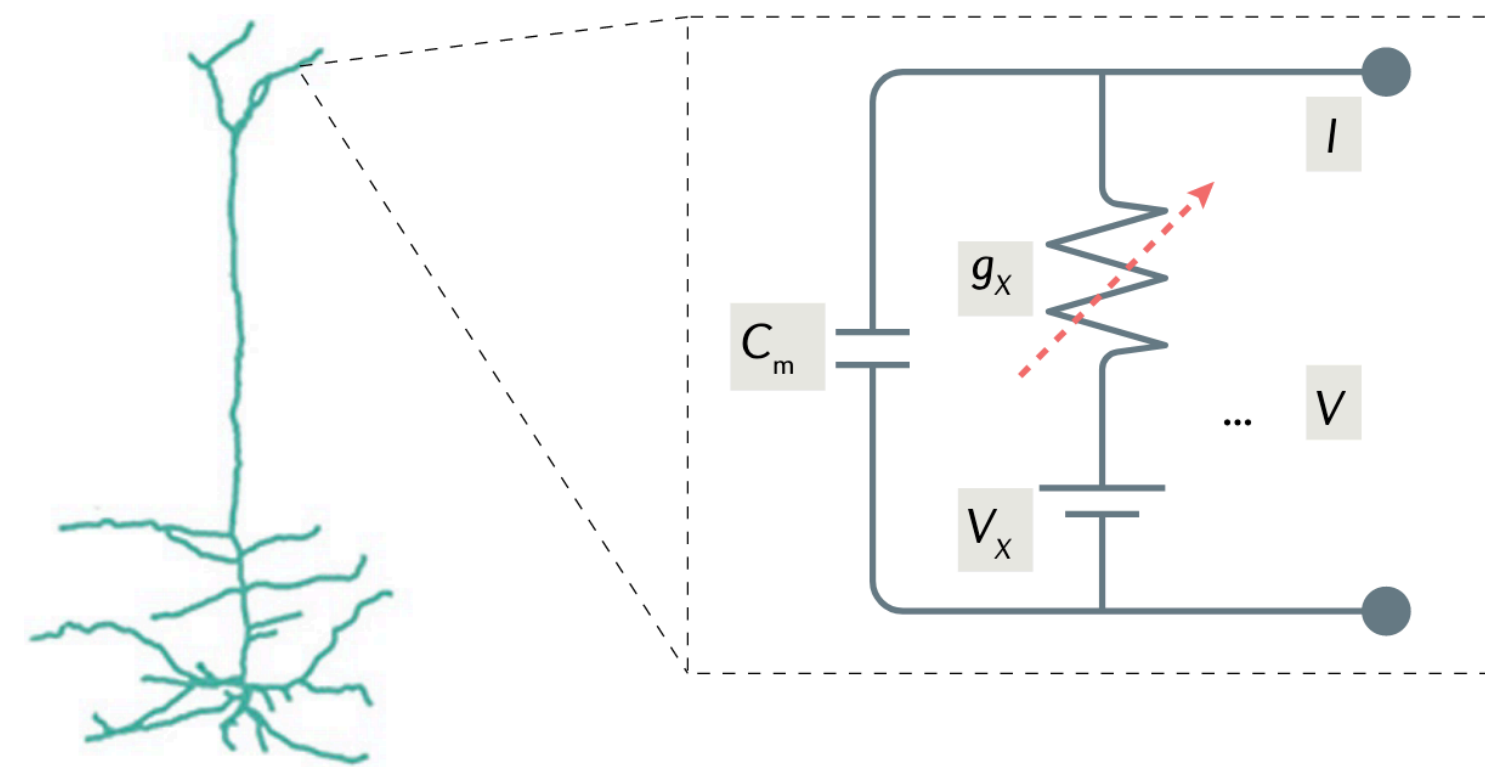
Larkum 1999

Precision of timing is required, the distal Ca^{2+} spikes and the bAP must occur within $\sim 10\text{-}30\text{ms}$



Computational models of dendrites

Illumination dendritic function with simulations



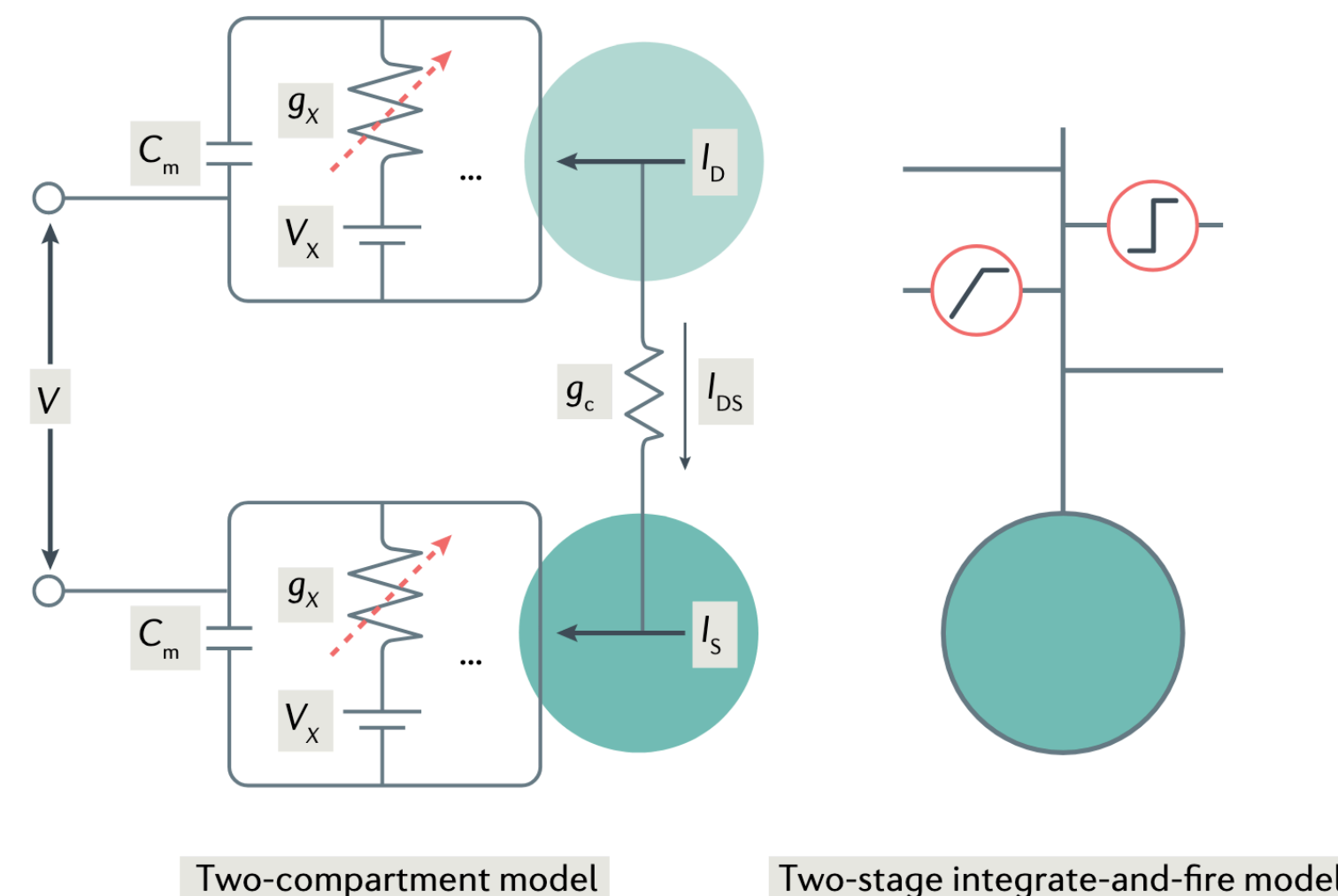
Multi-compartmental model

Reduced models allow for embedding the neuron in **neuronal microcircuits** and testing their **computational properties**

SST+ interneurons inhibit the apical dendrites of pyramidal neurons.
PV+ interneurons target the perisomatic regions of pyramidal neurons

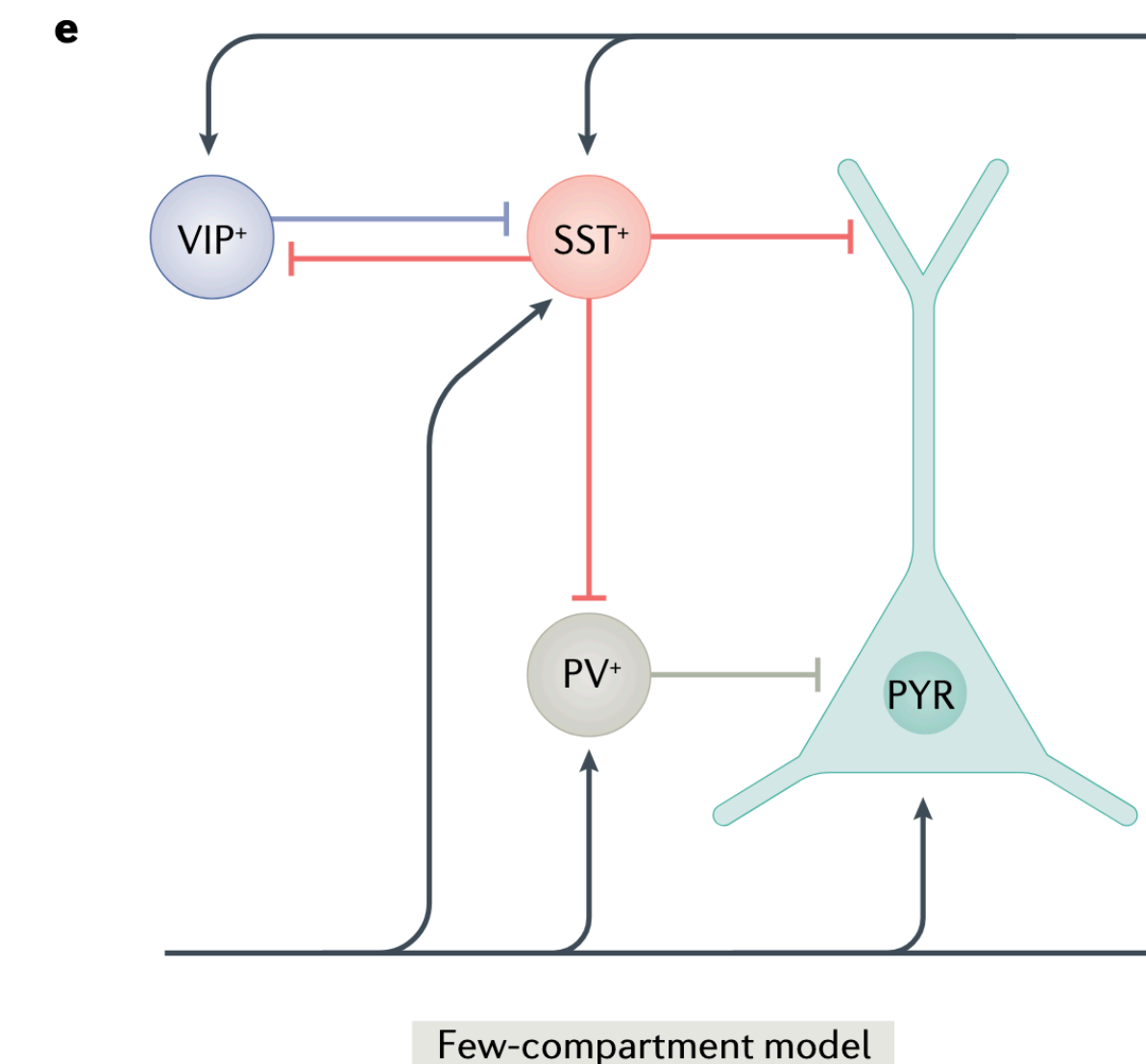
There is no single answer to the quest of finding the ‘best model’.

Single-neuron models with multiple-compartment dendrites can be used to assess **the effects of dendritic morphology, biophysics, and plasticity on neuronal output**.



Two-compartment model

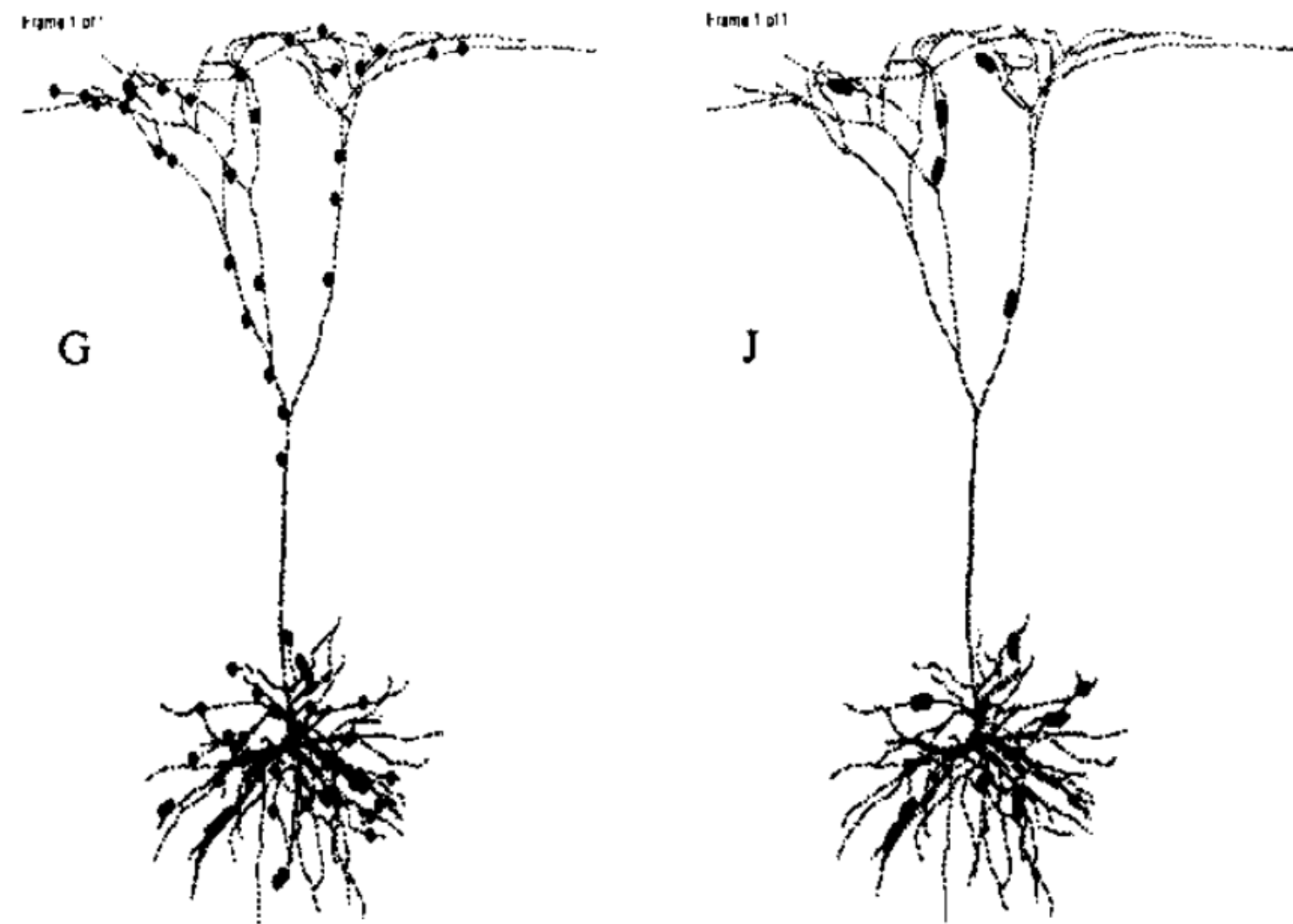
Two-stage integrate-and-fire model



Few-compartment model

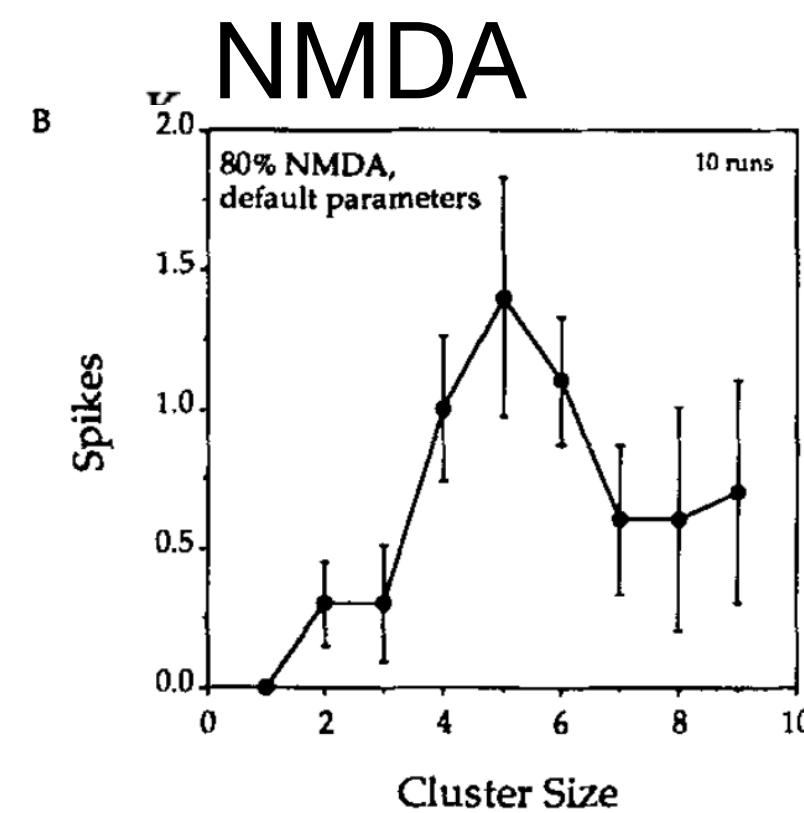
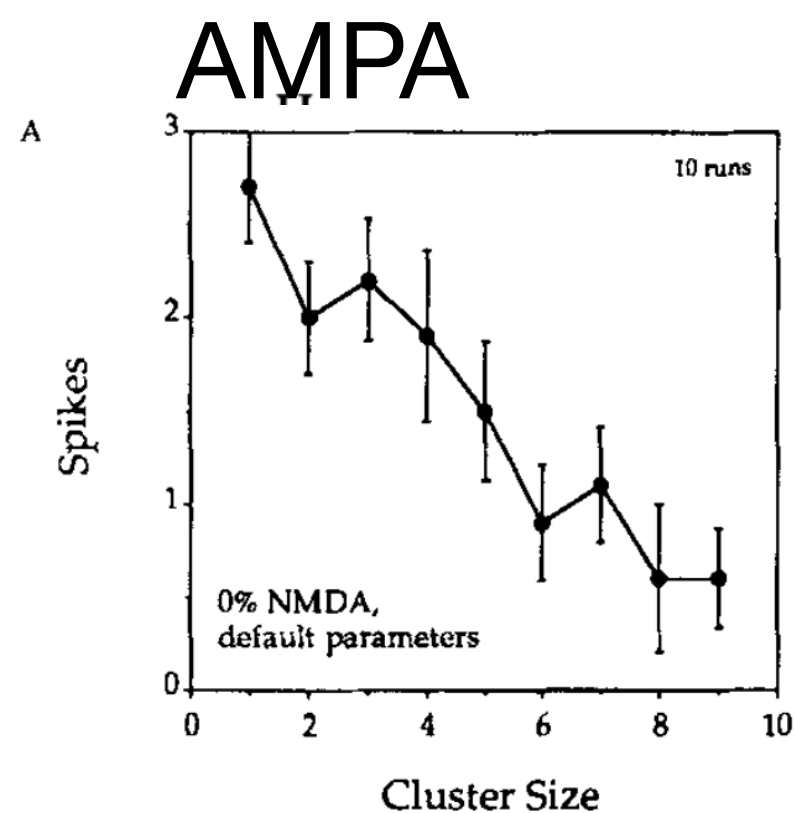
Realistic models of the dendritic tree

Precise synaptic locations and clustering predict NMDA *advantage*



Multiplicative interactions among groups of neighboring synapses greatly enhance the processing power of a neuron.

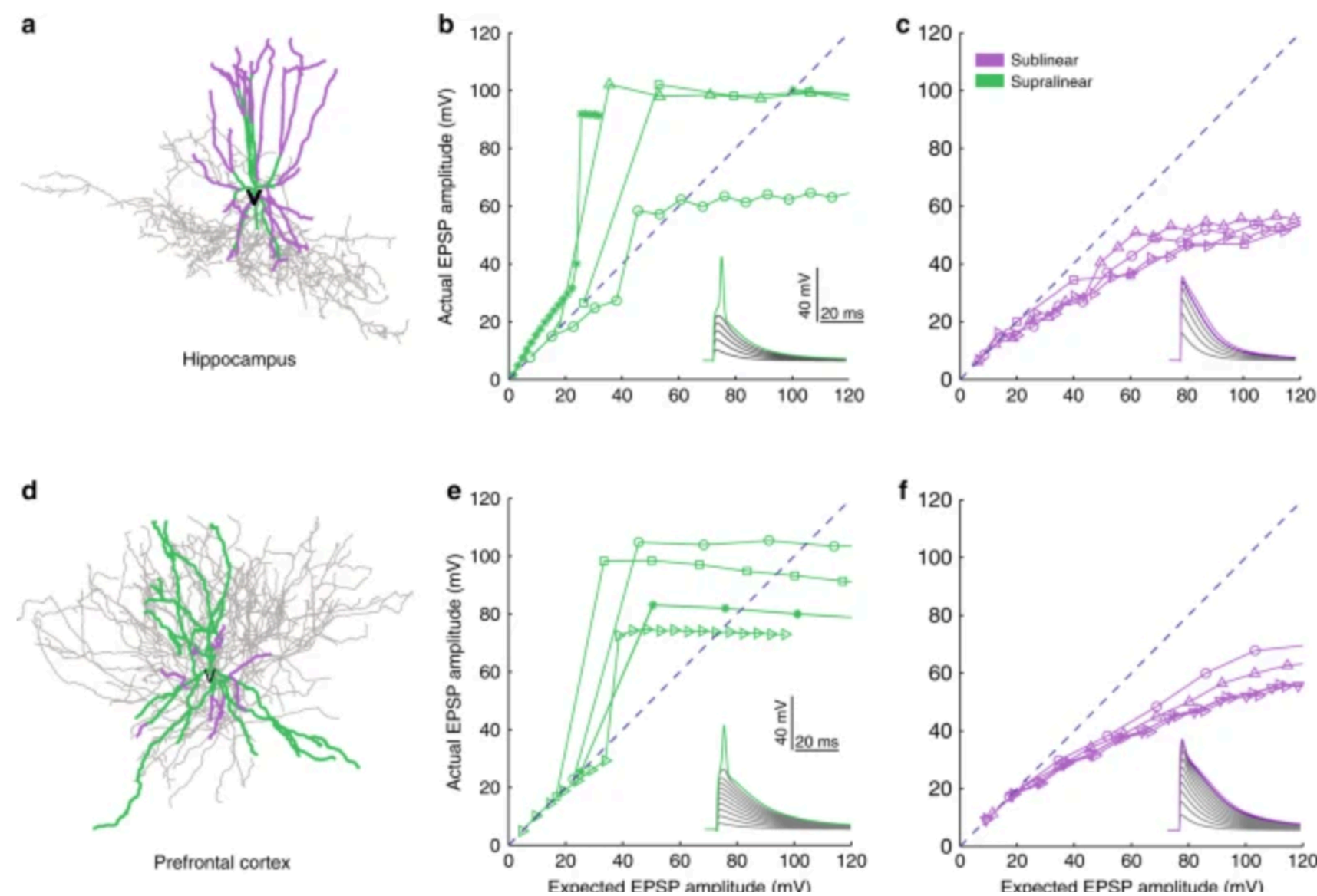
1. Large proportion of the excitatory synaptic input to dendritic spines is carried by NMDA channels
2. the pyramidal cell responds preferentially to spatially clustered, rather than random, distributions of activated synapses.
3. Second, based on this mechanism, the NMDA-rich neuron is shown to be capable of solving a nonlinear pattern discrimination task.



The spatial ordering of afferent synaptic connections onto the dendritic arbor is a possible biological strategy for pattern information storage during learning.

Realistic models of the dendritic tree

Non-linear integration in interneurons

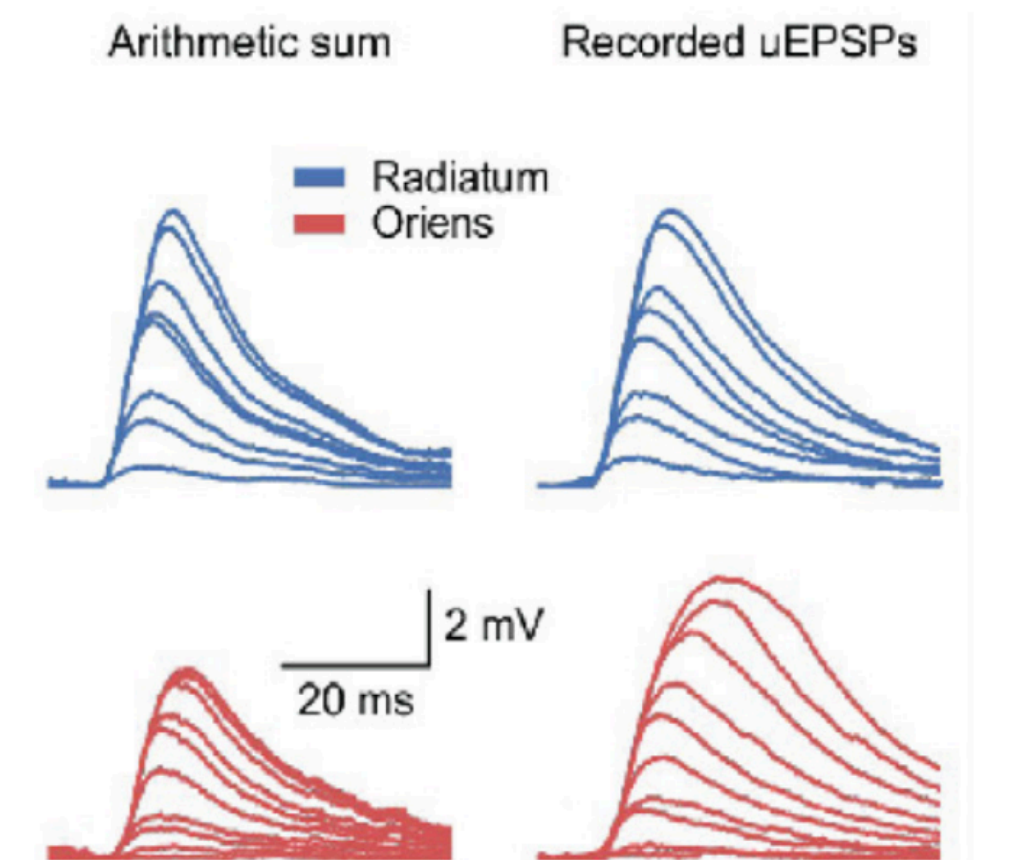


Different modes of synaptic integration can also coexist within the same dendritic tree.

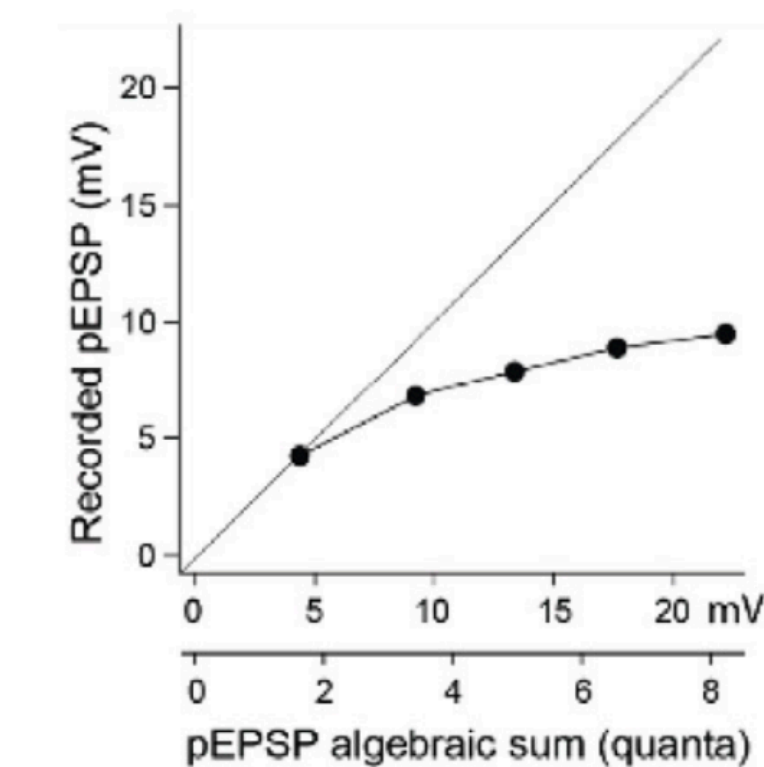
Computational modelling predicts that dendrites of both cortical and hippocampal Fast Spiking Basket Cells operate in one of two modes: supralinear or sublinear.

Experimental results:

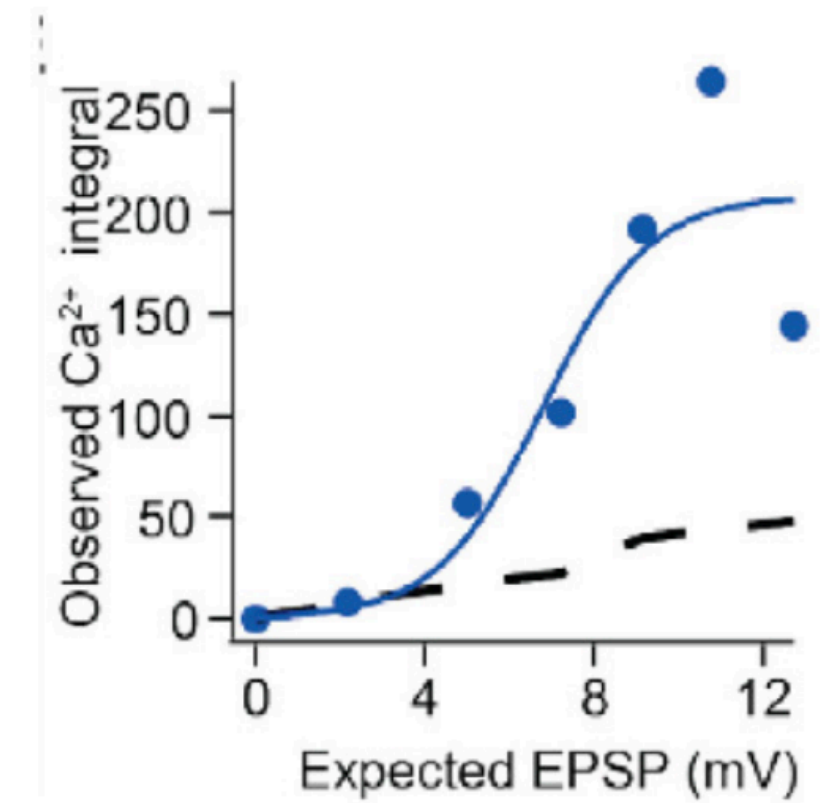
- CA1 PV+ INs have two types of dendrites: supralinear and linear.
- Cerebellar have sublinear EPSP summation but supralinear calcium accumulation.



CA1 str. radiatum and oriens PV



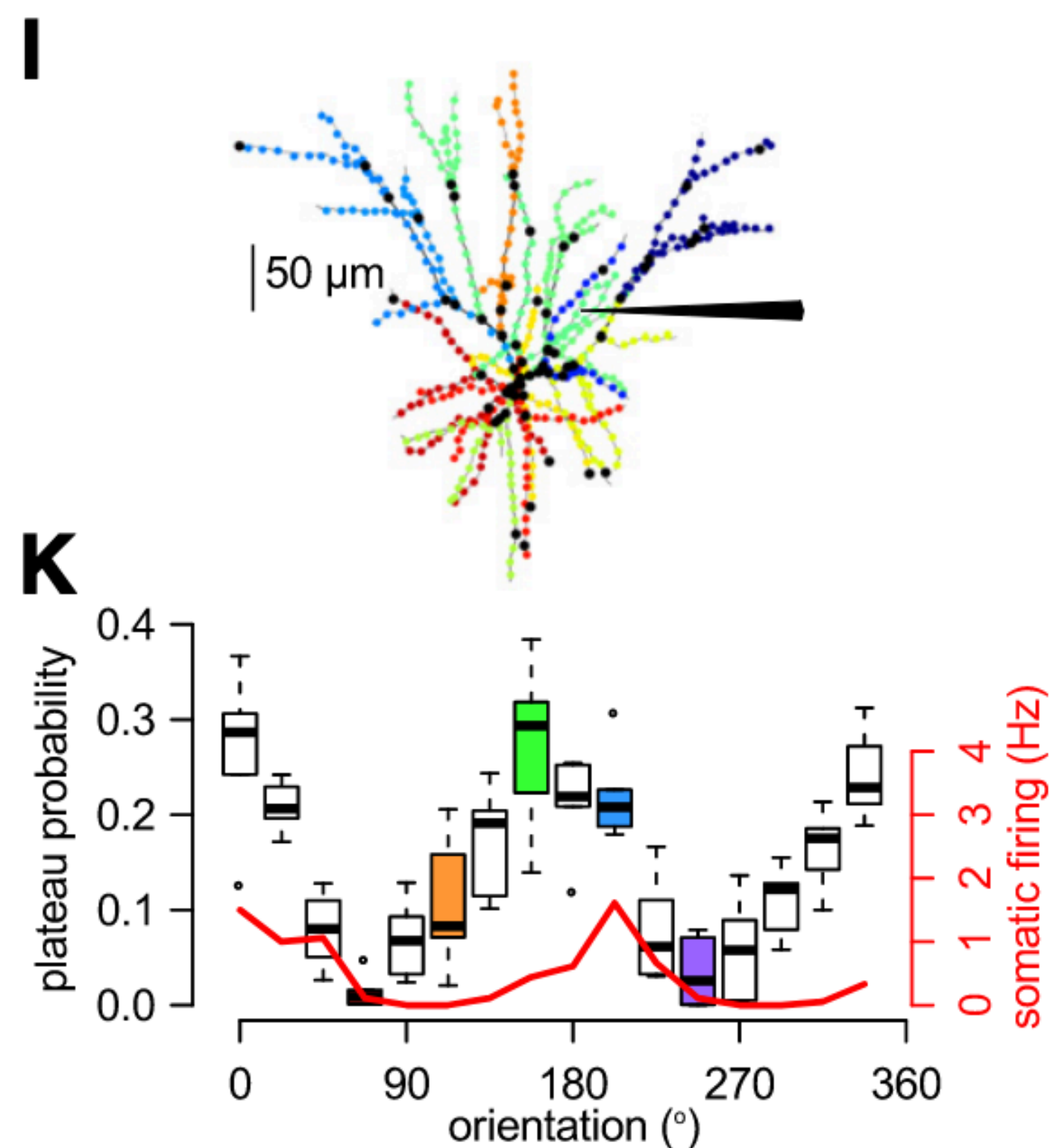
Cerebellar Interneurons (Stellate Cells)



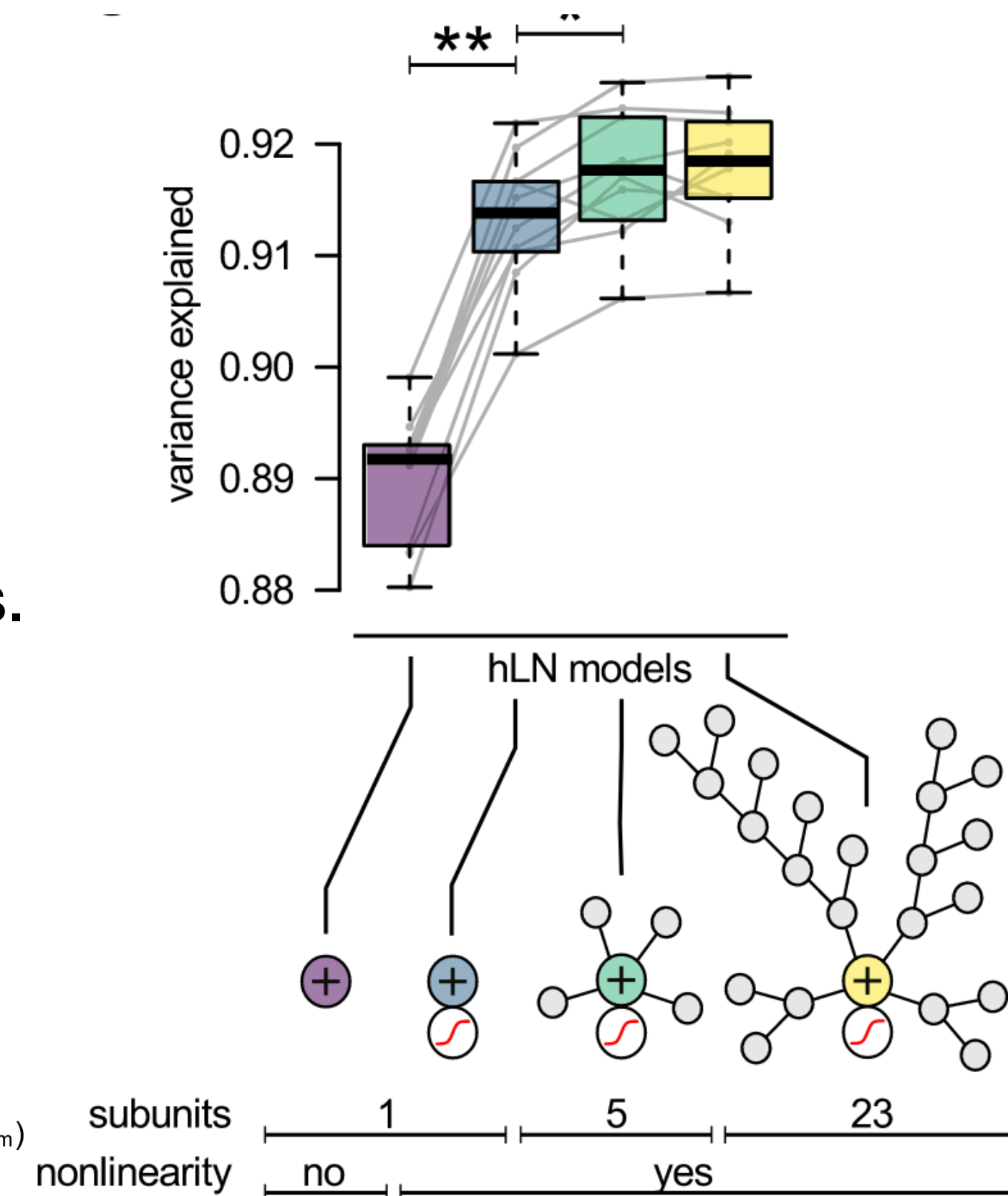
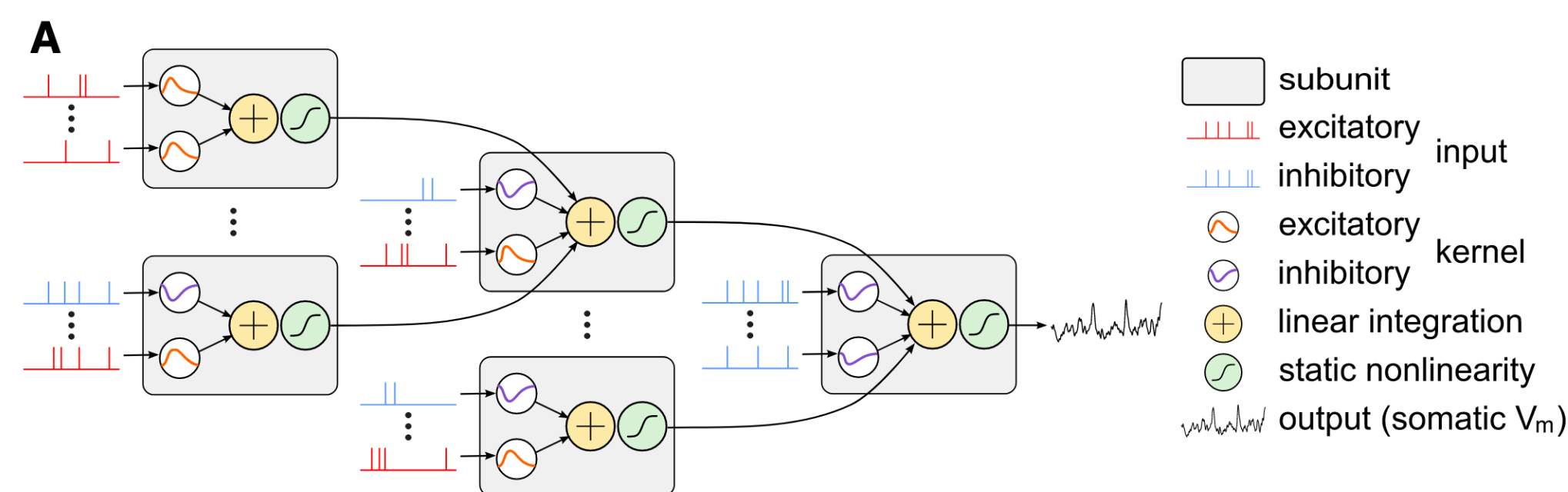
How many compartments?

A few non-linear compartments are enough

Synaptic bombardment smooths the effect of dendritic non-linearity



- Fit realistic neuron models to realistic inputs.
- Systematic reduction with hierarchical Linear-NonLinear units.
- Comparison of models with many or few units.



Reduced models of the dendritic tree

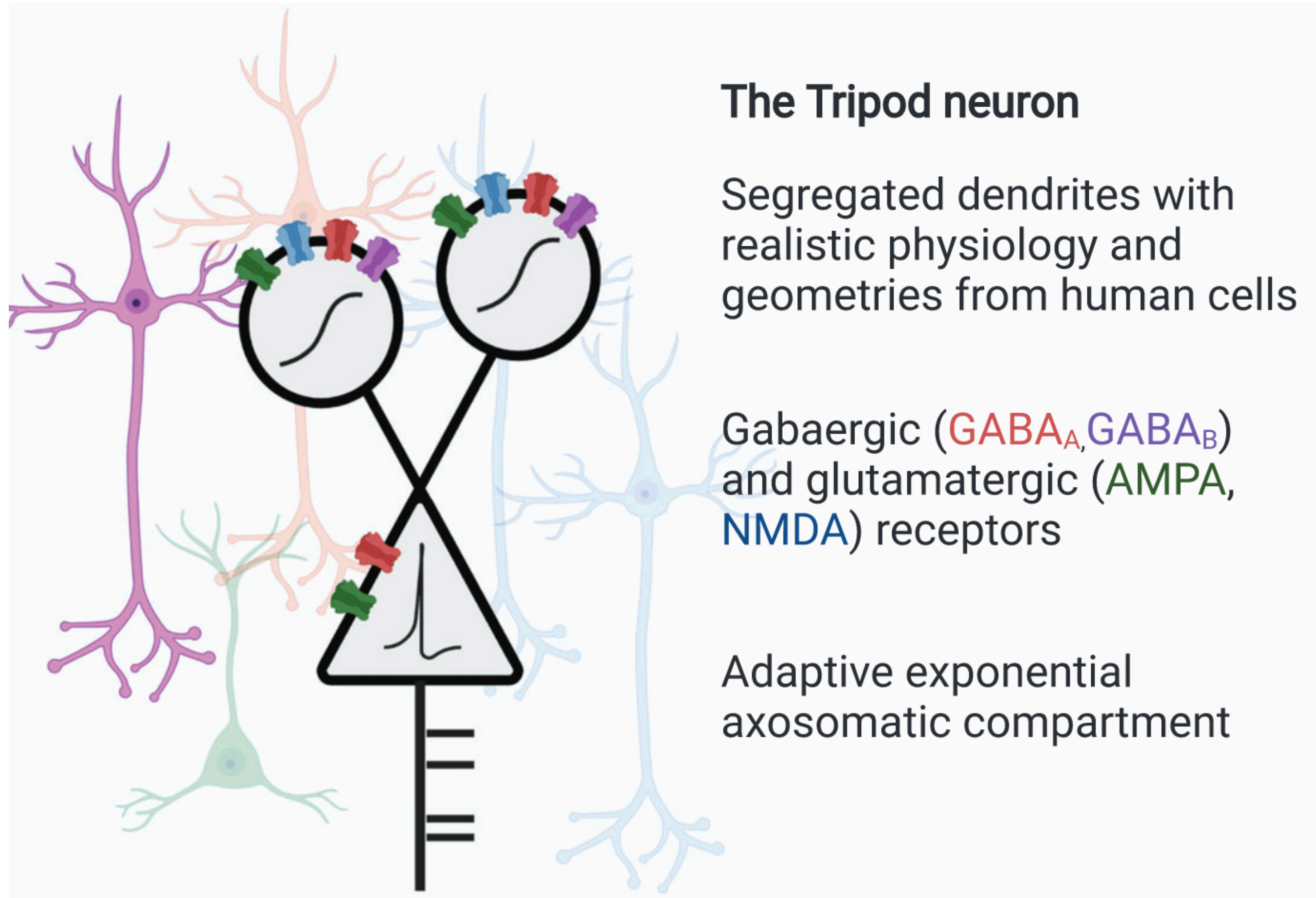
Few compartment models are composed of small sets of equations

The Tripod neuron

Segregated dendrites with realistic physiology and geometries from human cells

Gabaergic (**GABA_A**, **GABA_B**) and glutamatergic (**AMPA**, **NMDA**) receptors

Adaptive exponential axosomatic compartment



Quaresima, Fitz, et al. 2022

Soma compartment

$$\tau_m \frac{d}{dt} V_i(t) = -(V_i - V_r) + \Delta_T \exp\left(\frac{V_i - \theta}{\Delta_T}\right) + R I_d$$

Dendrite compartments

$$C_m^d \frac{dV^d}{dt} = -g_m^d (V^d - V_r) - \sum_k g_k(t) (V^d - E_k) - I_d \quad (3)$$

$$I_d = g_{ax}^d (V^d - V^s) \quad (4)$$

Synaptic conductance

$$g_k(t) = \bar{g}_k^{\text{syn}} \mathcal{N}_k \left(\exp\left(-\frac{t - t_0}{\tau_k^r}\right) - \exp\left(-\frac{t - t_0}{\tau_k^d}\right) \right)$$

$$g_{\text{NMDA}} = \bar{g}_{\text{NMDA}}^{\text{syn}} G(v)$$

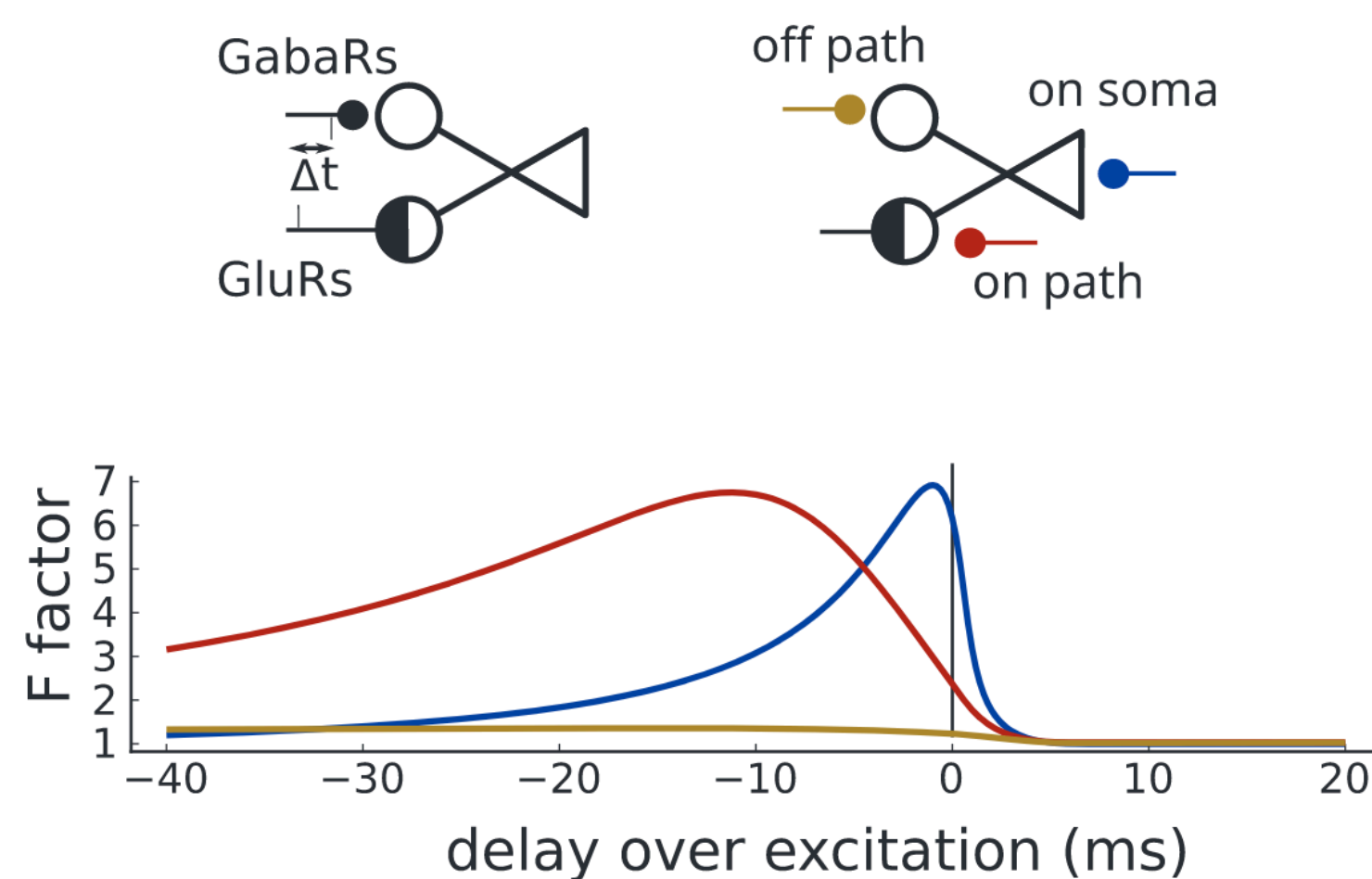
$$G(v) = \left(1 + \frac{C}{3.57 \mu\text{mol/L}} \cdot e^{-\gamma v} \right)^{-1}$$

Reduced models of the dendritic tree

The Tripod neuron reproduces dendritic integration and computations

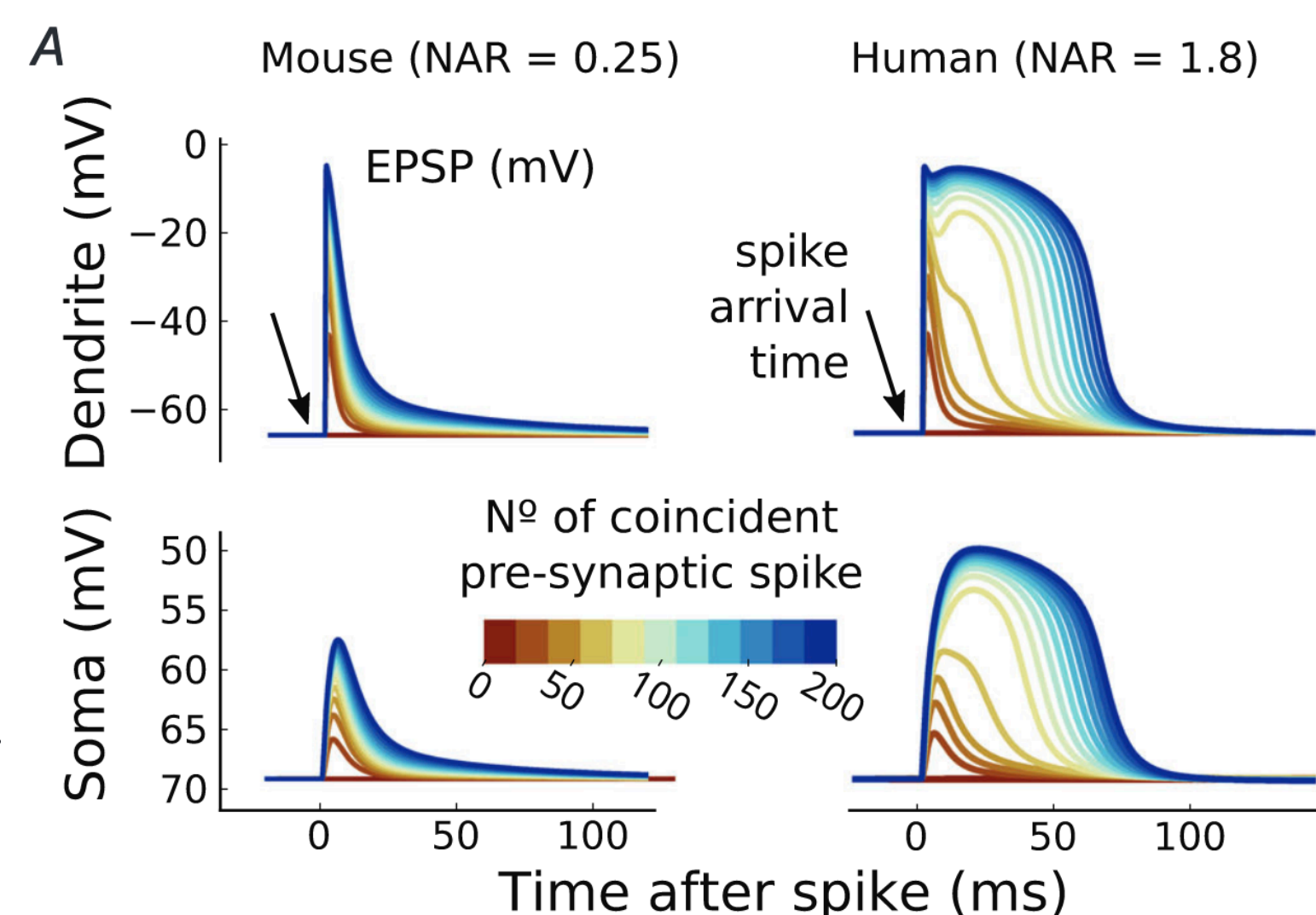
Passive cable effect

Inhibition over the same or different dendrite from excitation changes the somatic response.



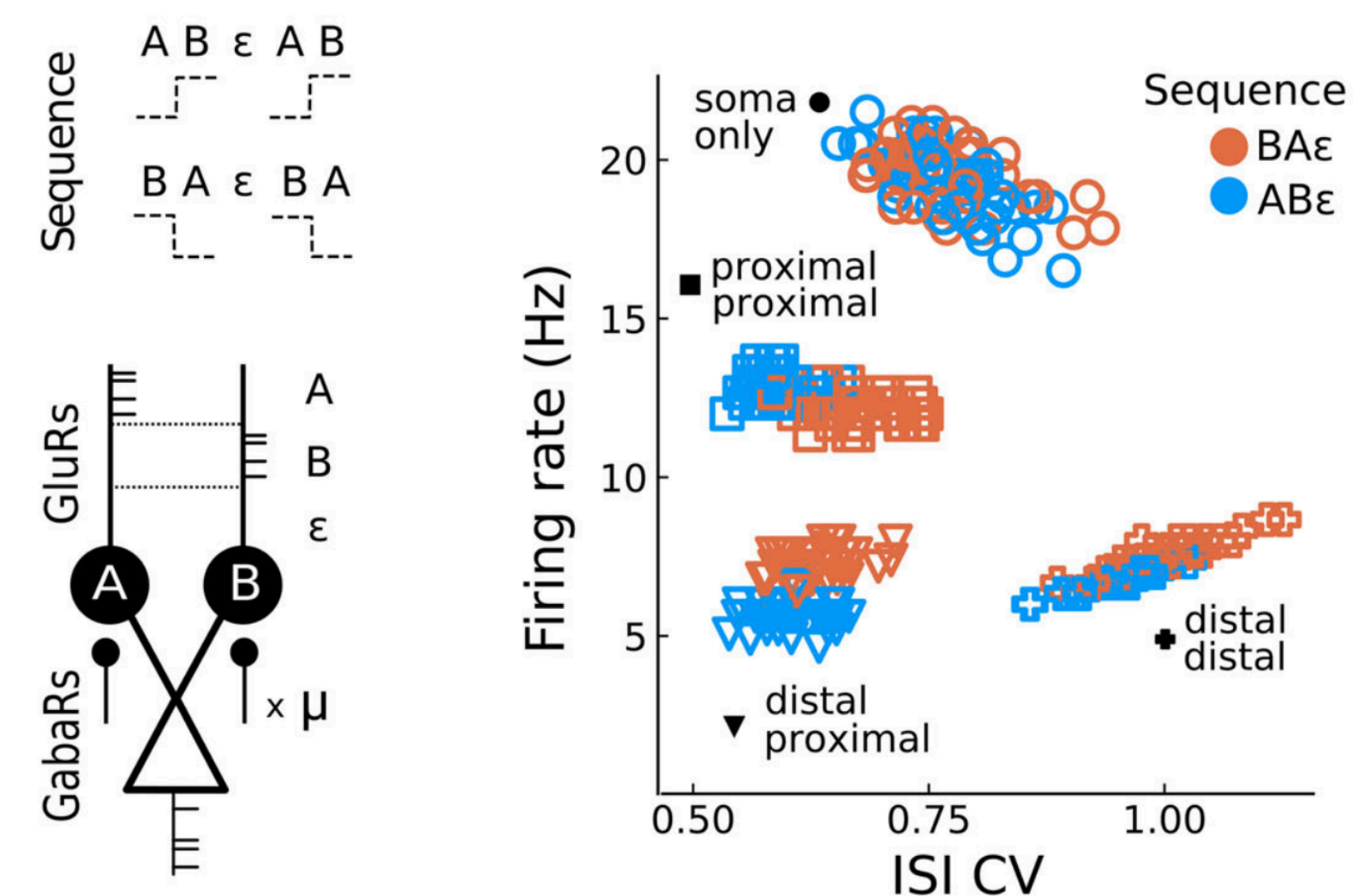
Dendritic non-linearities

The Intensity and duration of NMDA spikes depend on geometry and the concentration of NMDA receptors.



Dendritic computations

The model increases the computational capabilities of single-cells. It introduces a spike-silent dendritic memory



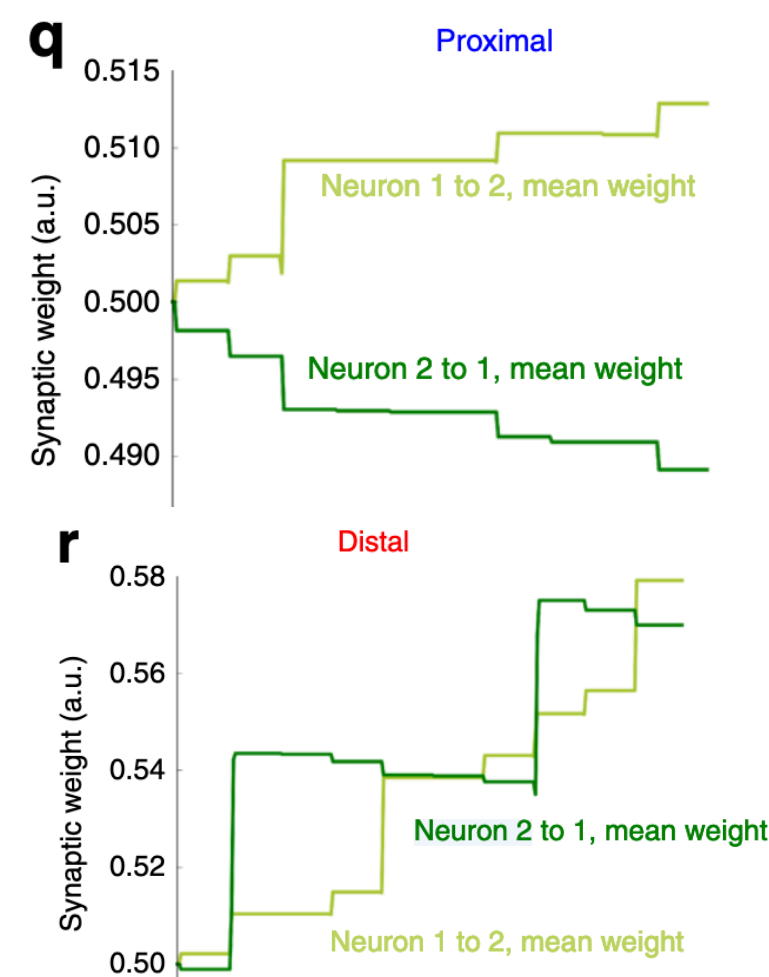
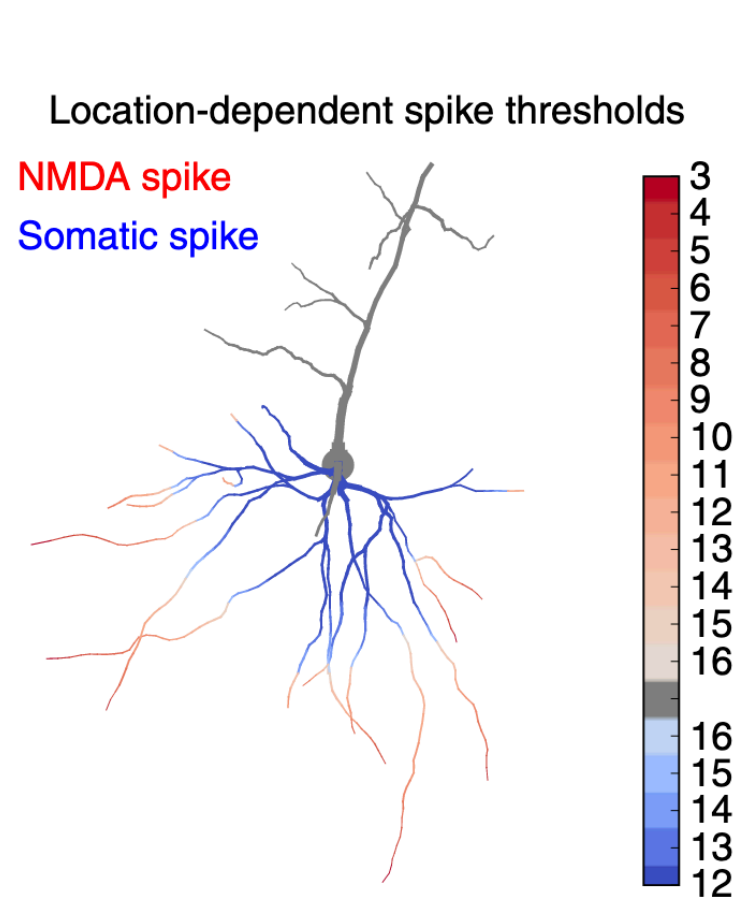
The impact of dendrites on memory and learning

Dendritic engram

Dendrites integrate synaptic inputs in non-linear ways, affecting the formation and retrieval of memories.

Voltage-dependent plasticity

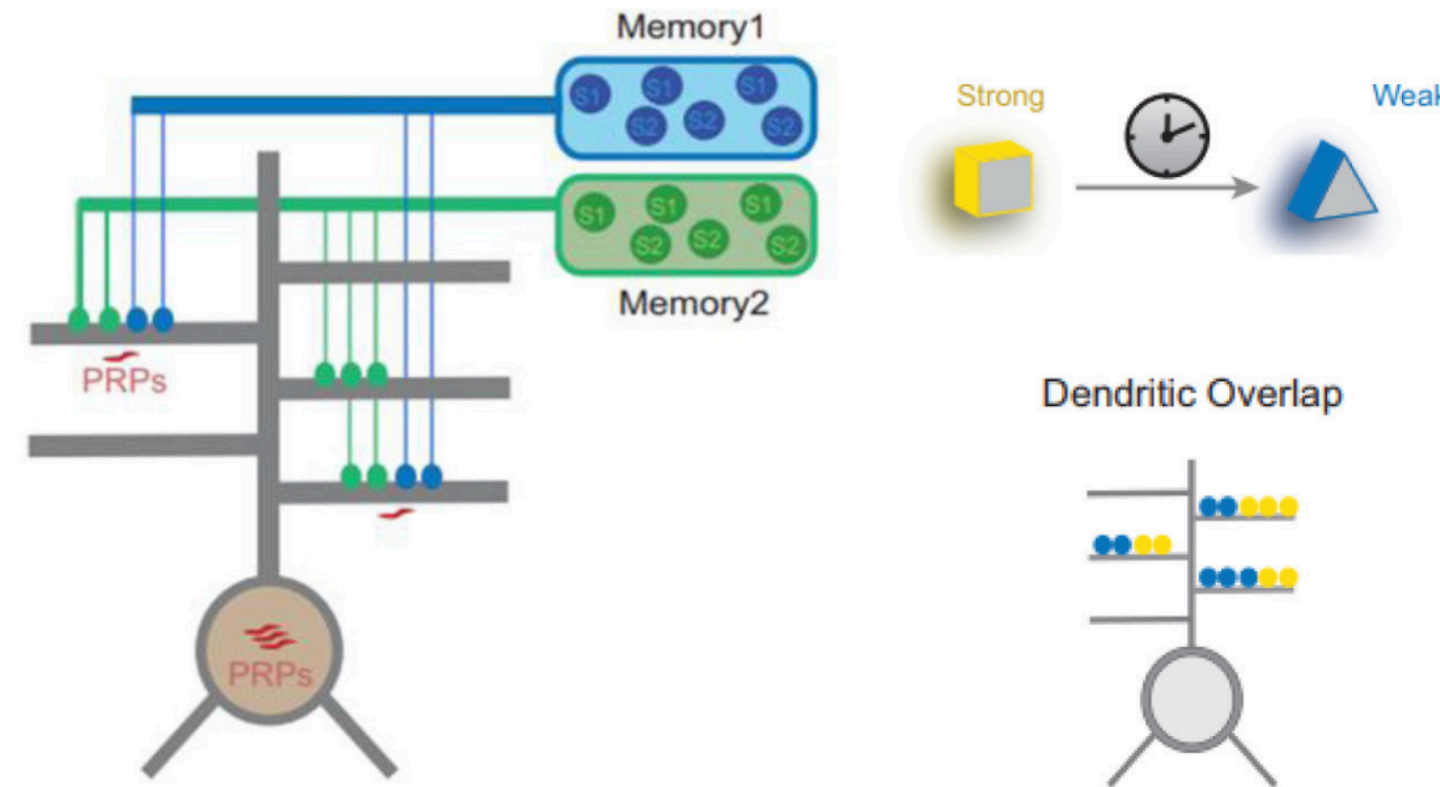
Potential/Depression depends on synaptic location and dendritic depolarization.



Bono & Clopath (2019)

Memory clustering

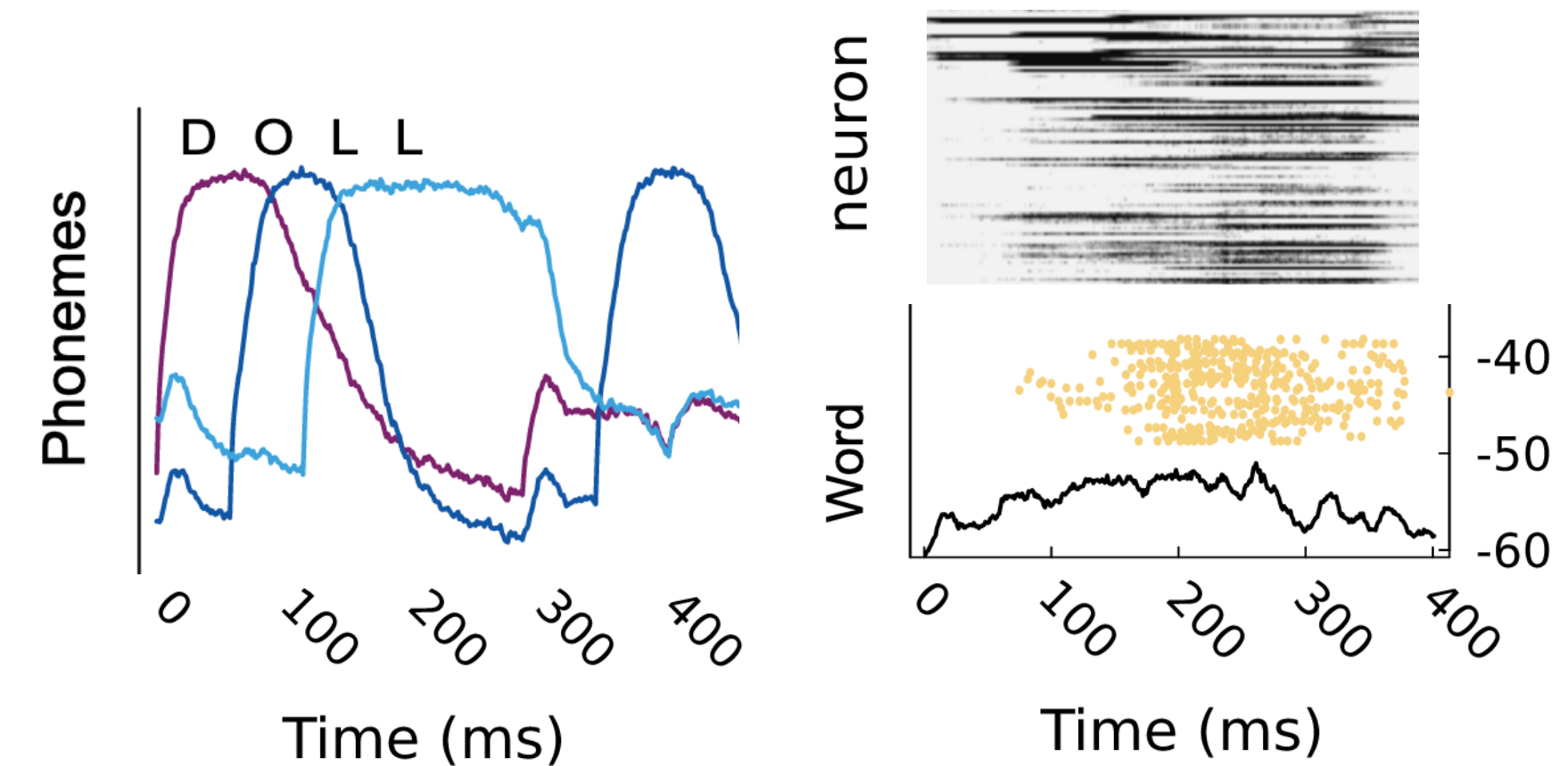
Different memories can be associated by clustering on the same branch.



Kastellakis & Poirazi (2015)

Sequence learning and retrieval

Dendritic engrams support the retrieval of overlapping memories via dendritic memory



Quaresima, Fitz et al. (2023)

Information processing in dendrites

Dendritic arborization makes up the many aisles of the Telegrapher's building.

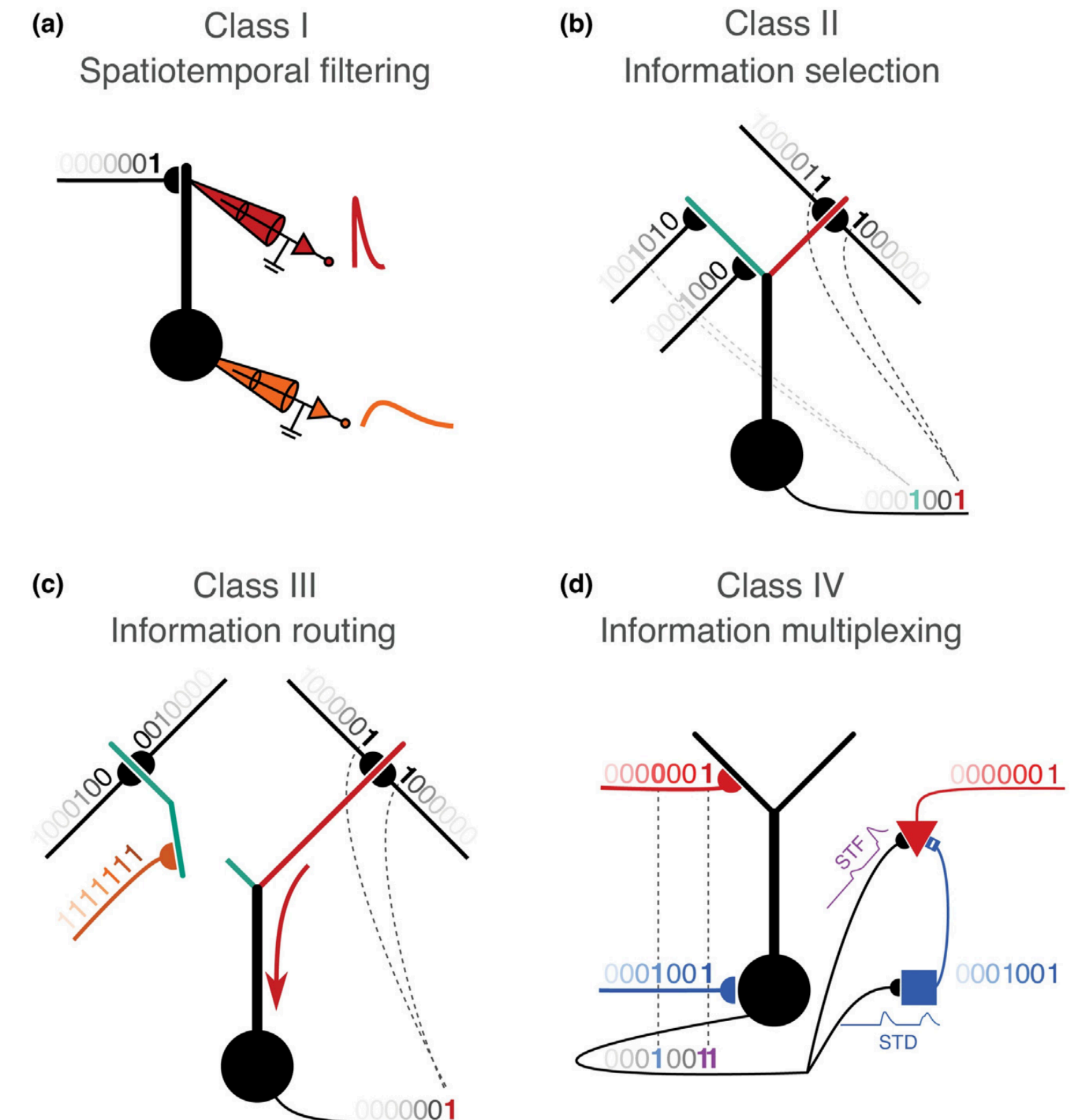
A coherent view of their algorithmic power and how they may contribute to neural network models.

Spatio-temporal filtering: Location-dependent attenuation and filtering combined with linear summation.

Information selection: Nonlinear amplification mechanisms select the information that determines the cell's output.

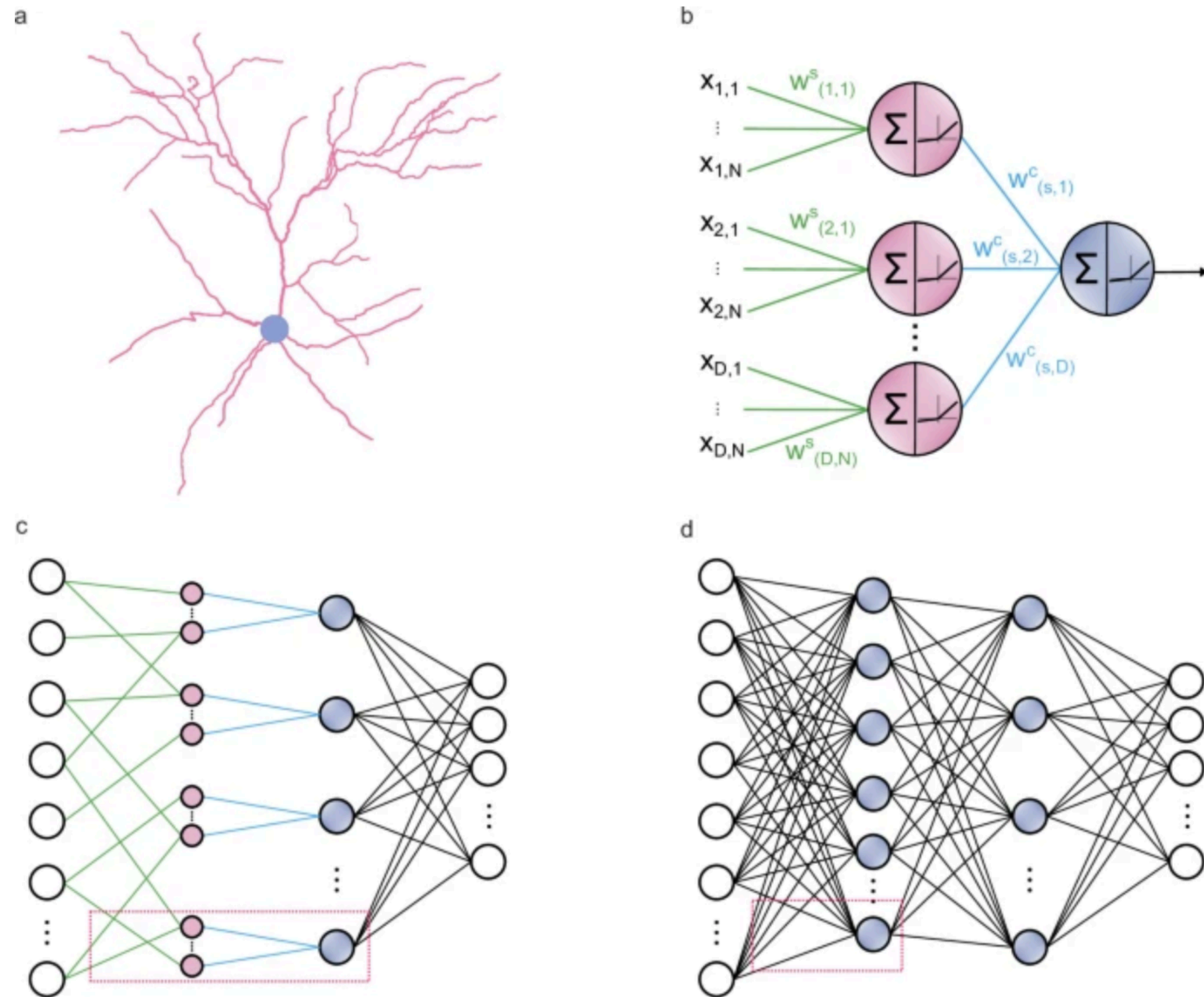
Information routing: Spatial distribution of excitation and inhibition selects which input pathway is active.

Information multiplexing: Dendritic-driven bursts represent multiple inputs into one spiking output,



Dendrites in Deep Neural Networks

Dendrites lead to accurate, robust and parameter efficient learning



Chavlis & Poirazi (2019)

Dendrites as an additional layer that provides weighted inputs to the somatic nodes.

dANNs are constructed as typical ANNs with two hidden layers, in which the first (dendritic) layer is connected in a sparse and structured manner to the second (somatic).

$$\text{Boolean mask: } \mathbf{W}_k \rightarrow \mathbf{W}_k \odot \mathbf{M}_k$$

ANN architectures that incorporate the structured connectivity limit the number of trainable parameters, and counteract overfitting.

Two reasons:

- ▶ dANN models form primarily **mixed-selective nodes**.
- ▶ Define a scheme for **weight sparseness**.

Computational models of dendrites

Tools to simulate multi-compartment neurons.

Dendrify allows for the integration of dendrites in Brian2 simulations. It focuses on neurons with few compartments

Neuron supports simulations of detailed multicompartment models. The construction of a neuron is fairly complex.

SpikingNeuralNetwork.jl allows for custom-definition of multi-compartment neurons, and it includes the Tripod in the model library.

